

# Byzantine fault tolerance for peer-to-peer collaboration

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# COLLABORATIVE APPLICATIONS

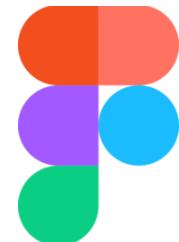
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Google Docs



Office 365

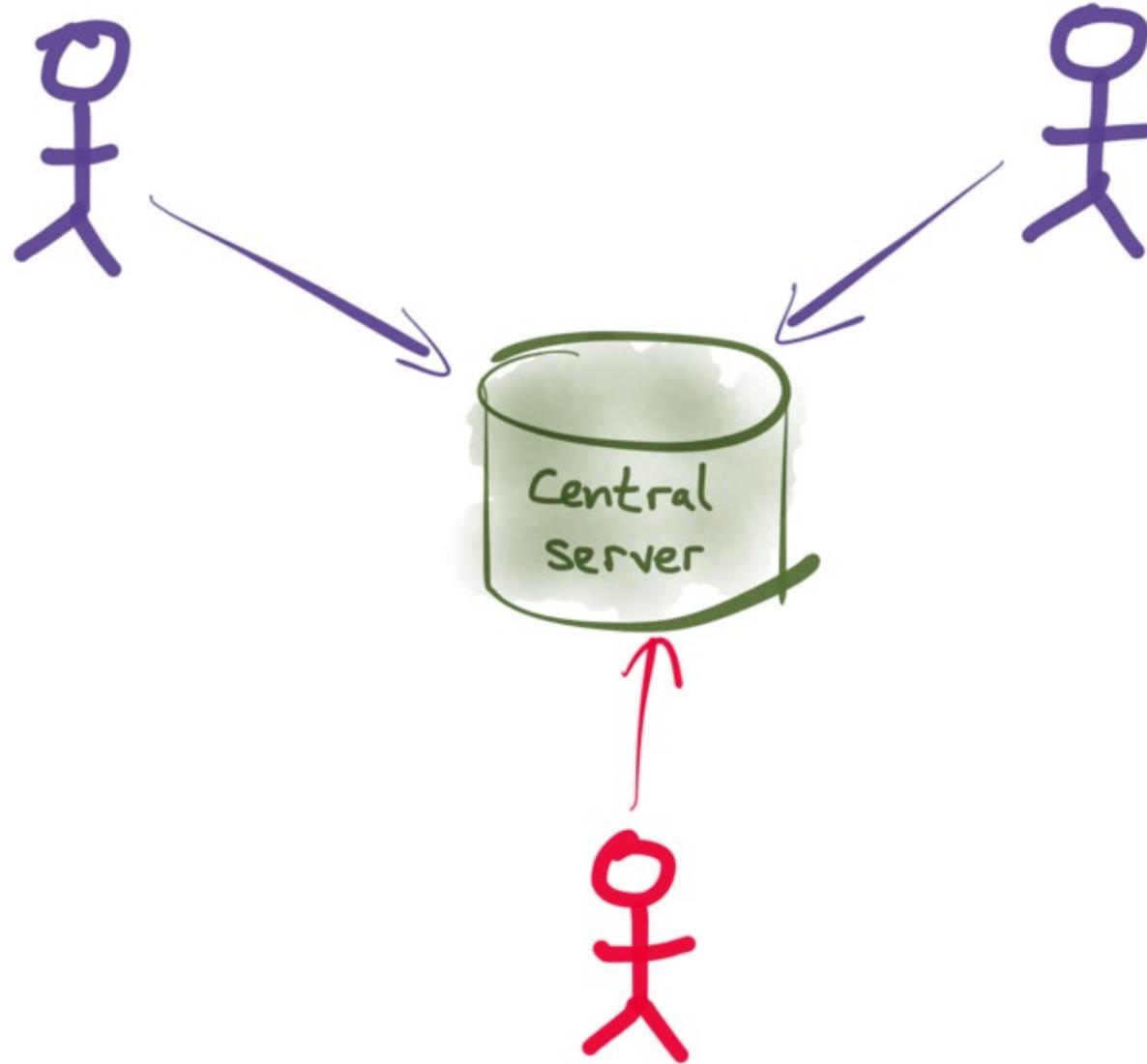


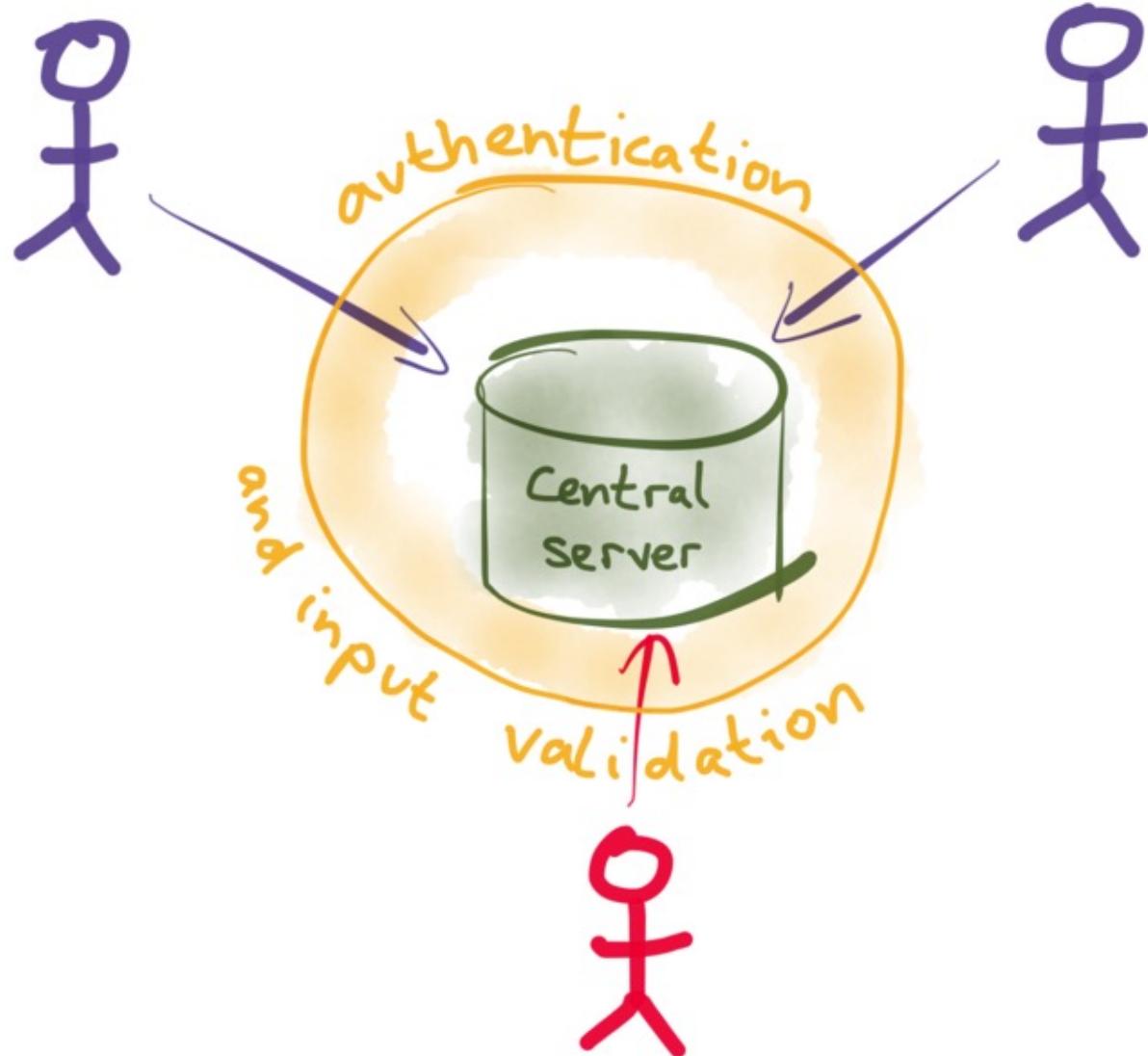
Figma

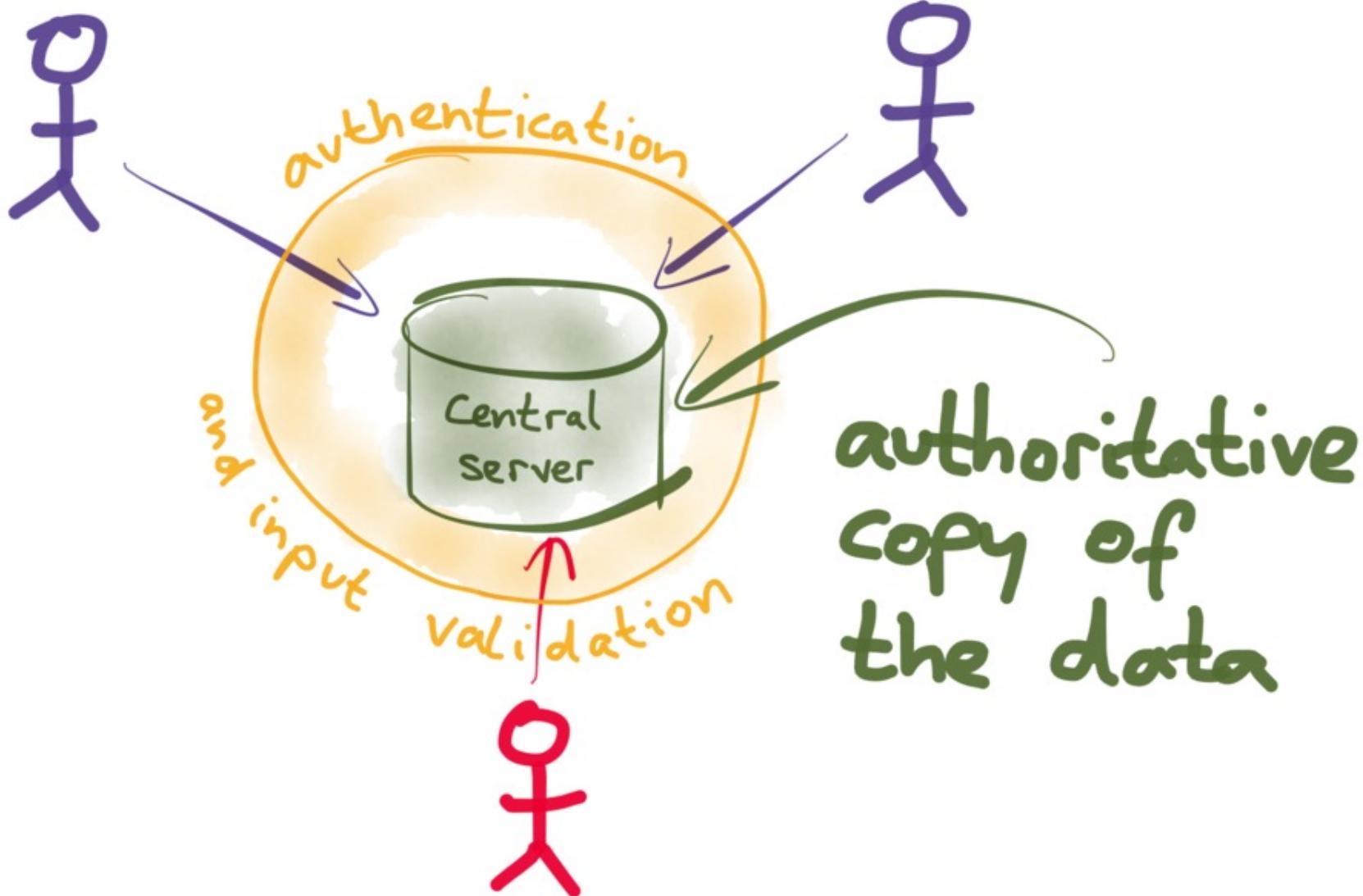
Wide range of domain-specific collaboration software, e.g. for investigative journalism, medical records, data analysis, engineering/CAD, ...

## Byzantine fault tolerance:

System continues to provide its advertised guarantees, even if some nodes are **malicious** (do not correctly follow protocol).

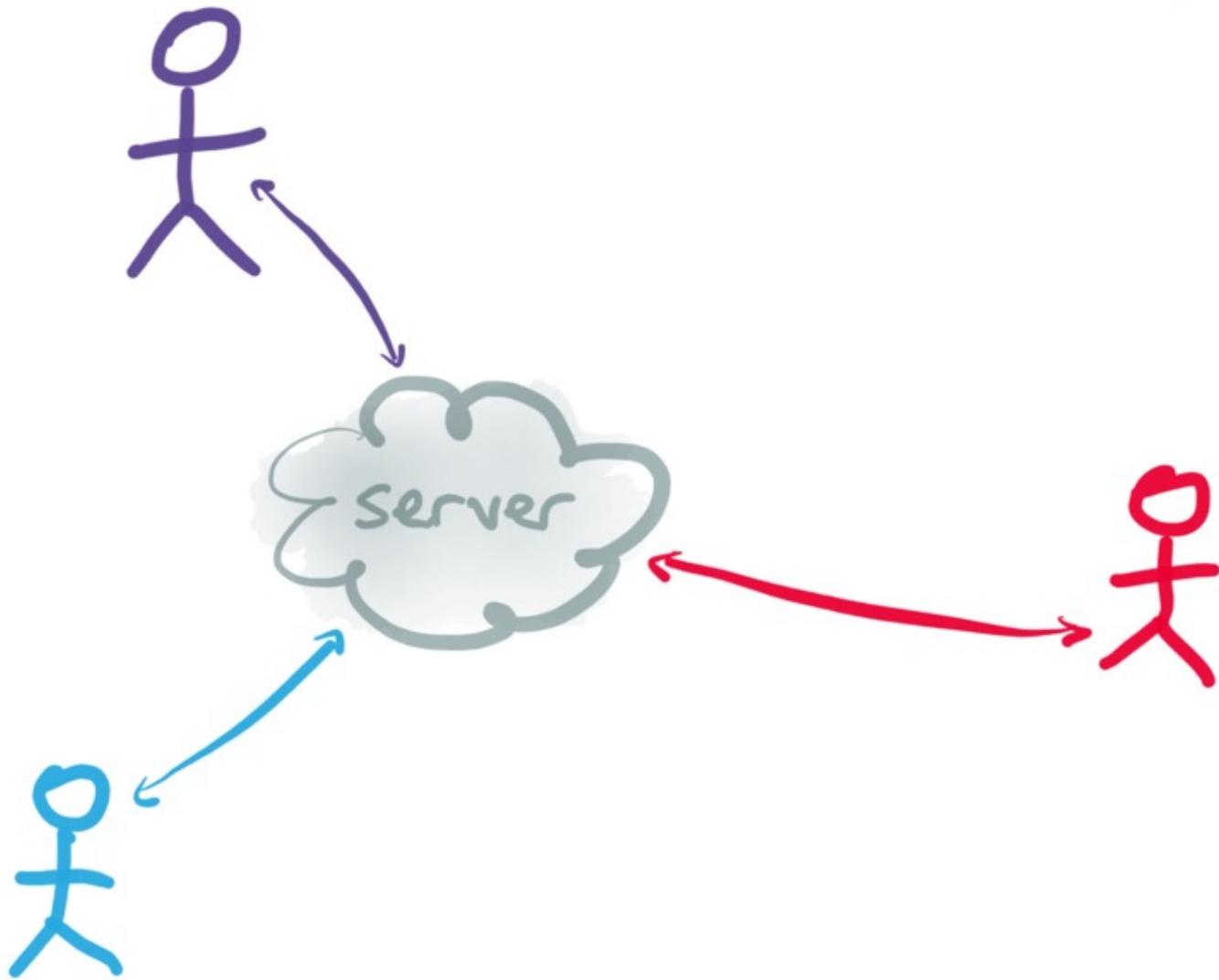






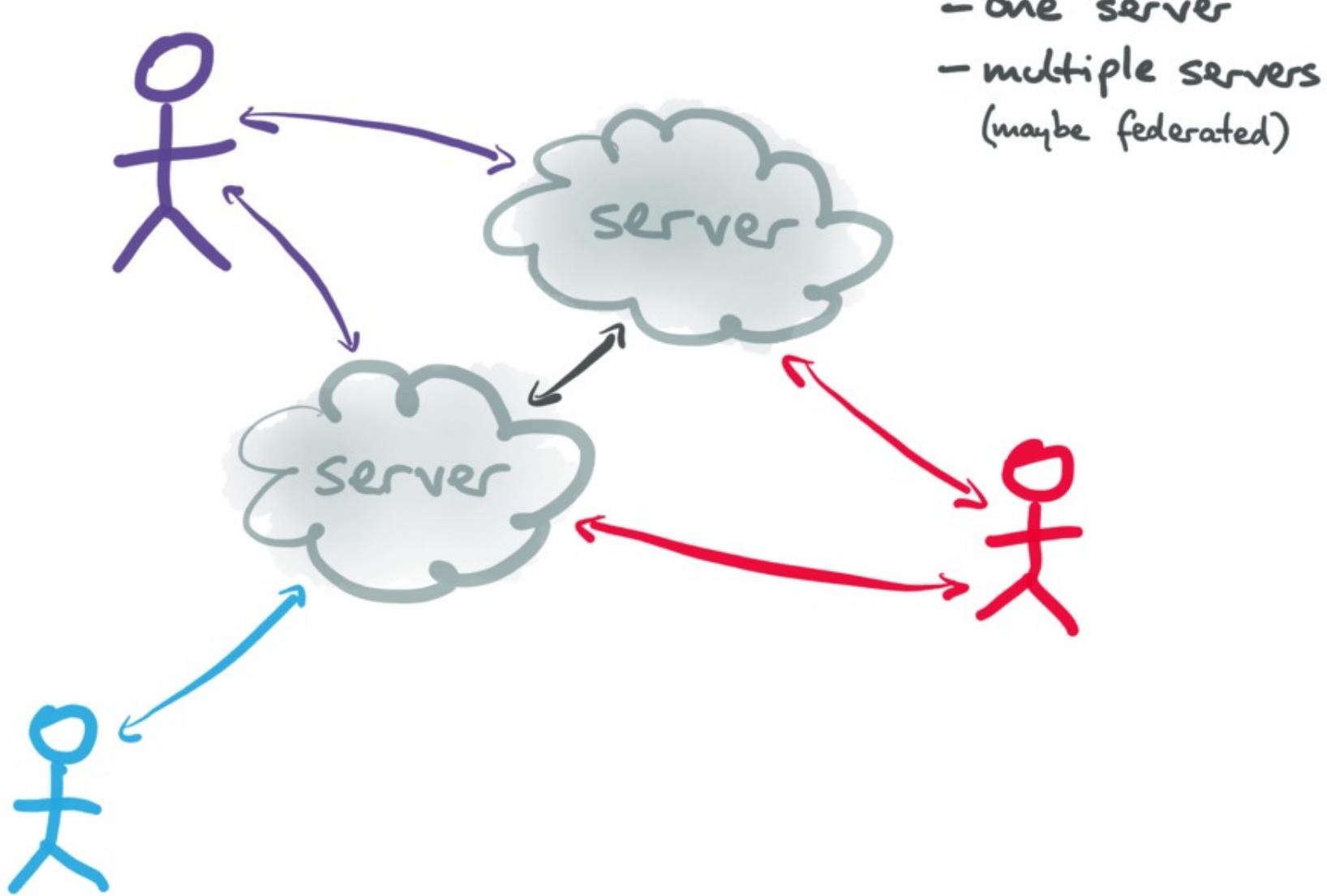
# COLLABORATION IN ANY NETWORK TOPOLOGY

- one server



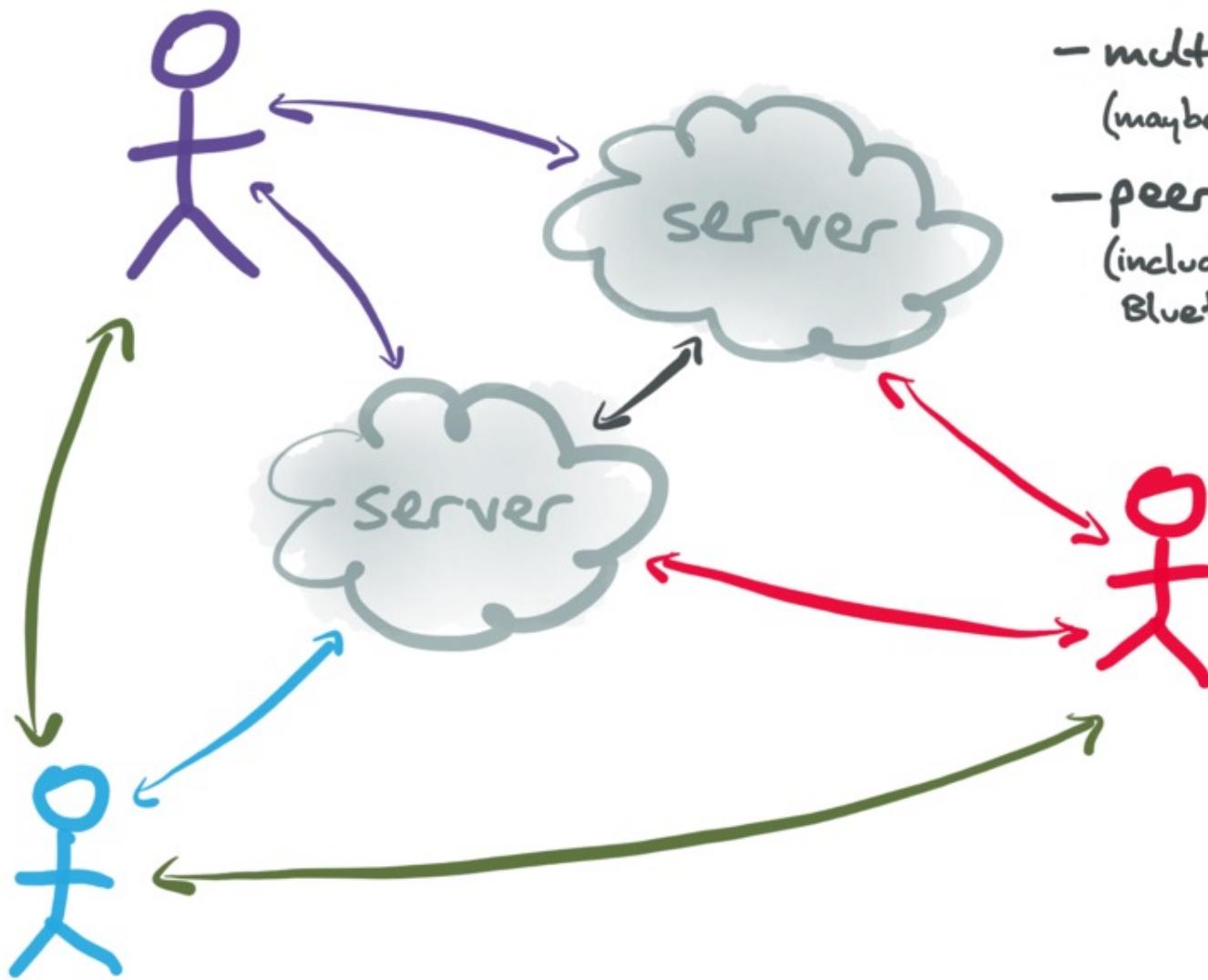
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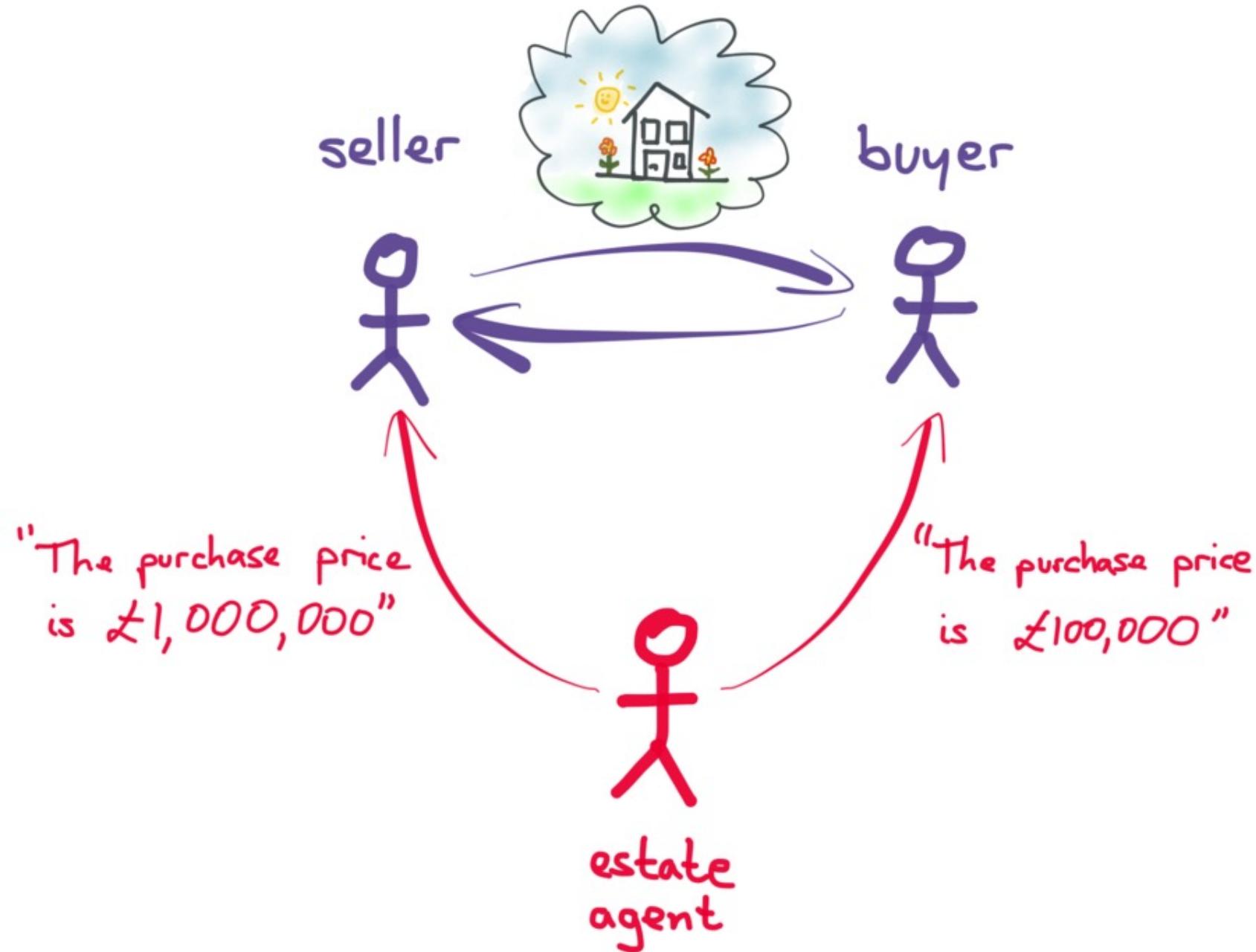


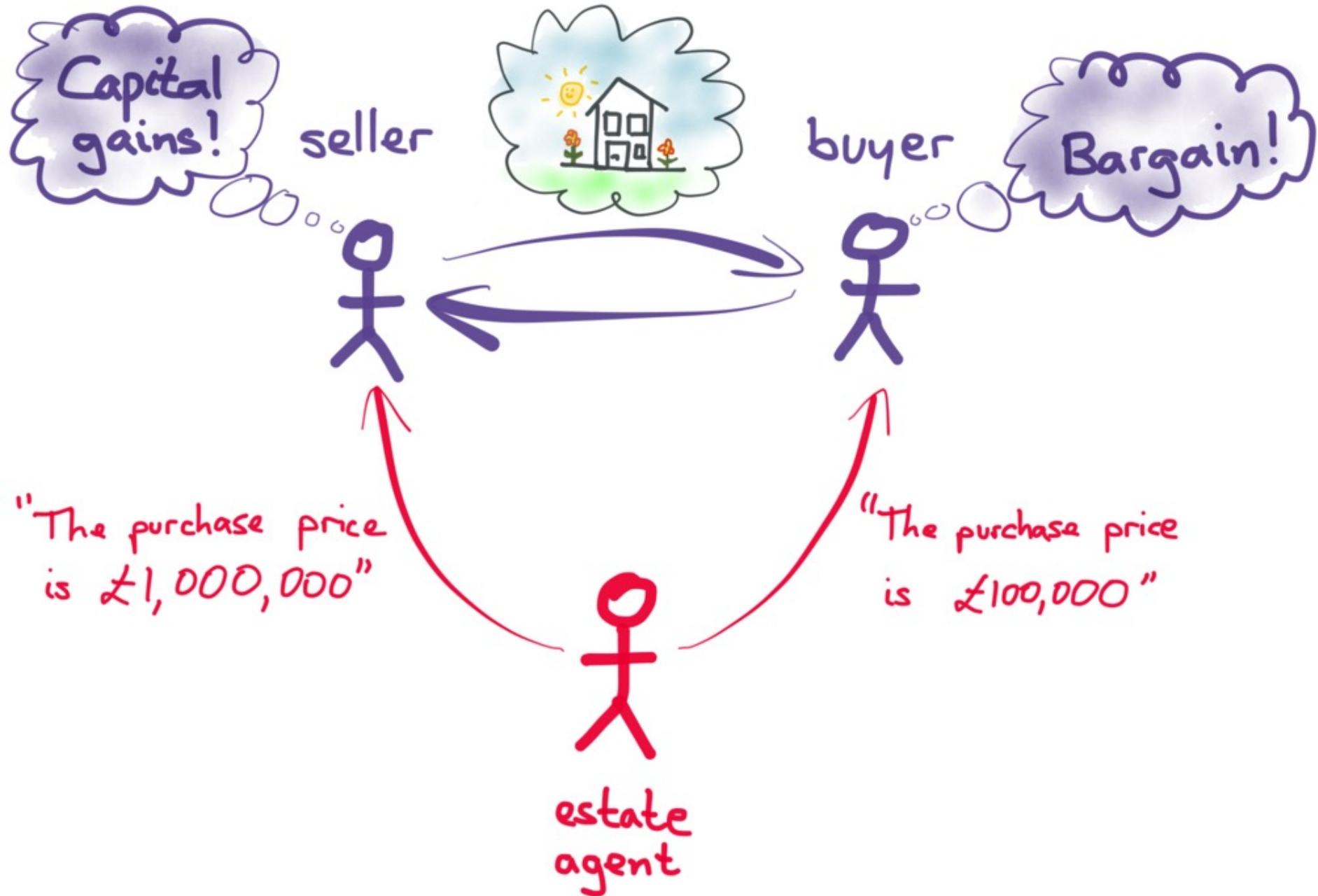
- one server
- multiple servers  
(maybe federated)
- peer-to-peer  
(including LAN, Bluetooth, etc.)

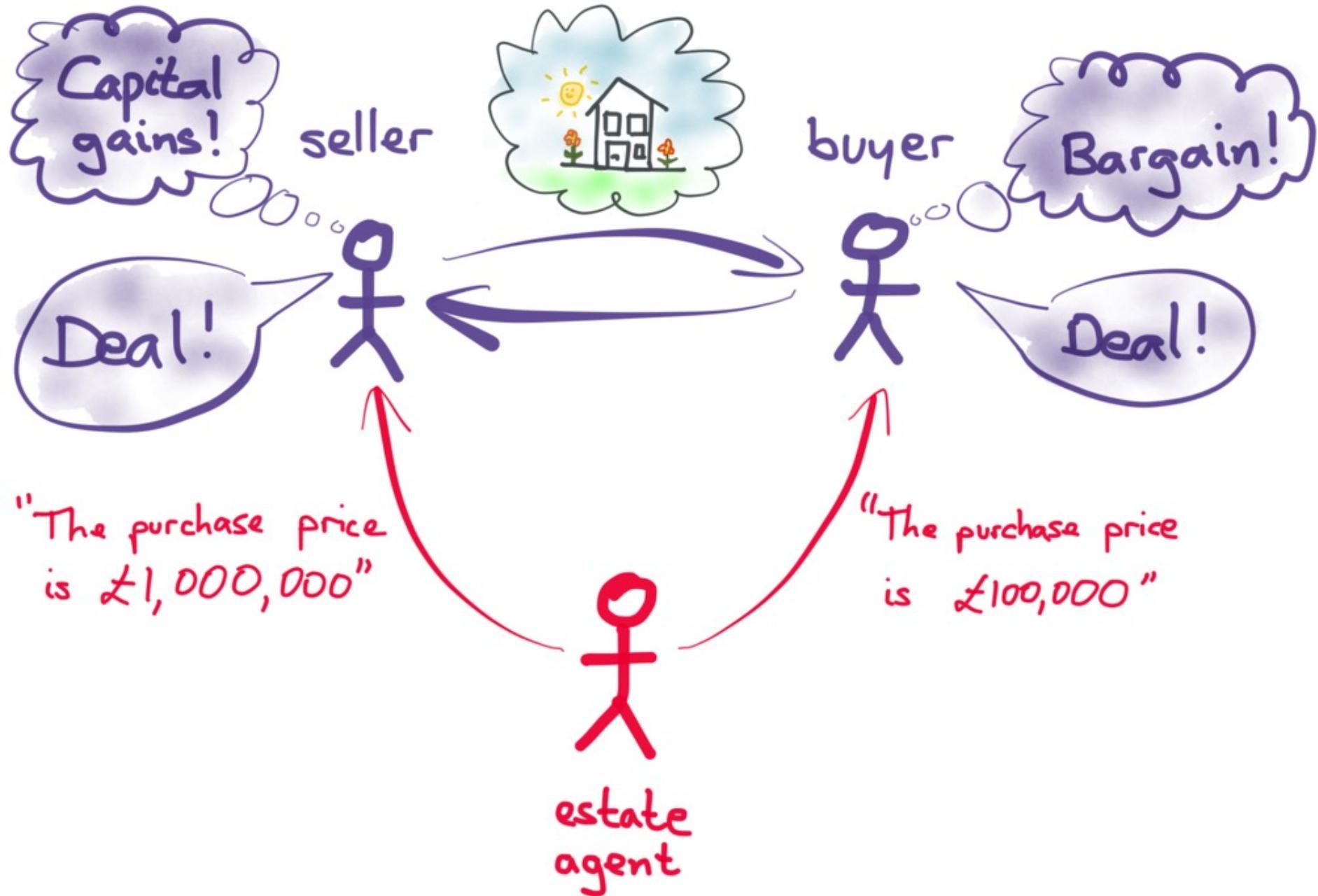




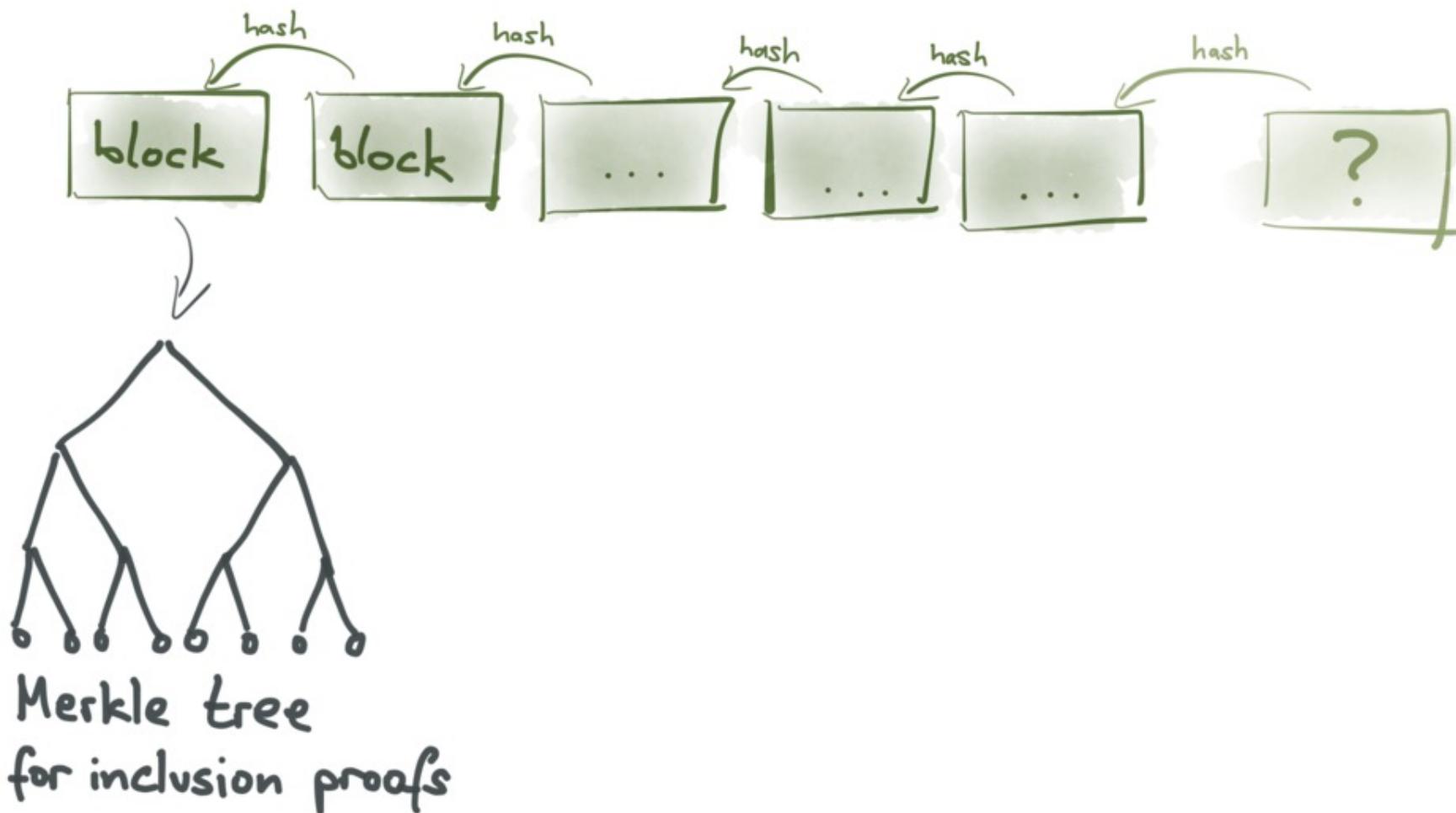
A red stick figure with a large head and a single eye, standing below the transaction diagram. Below the figure, the words "estate agent" are written in red.



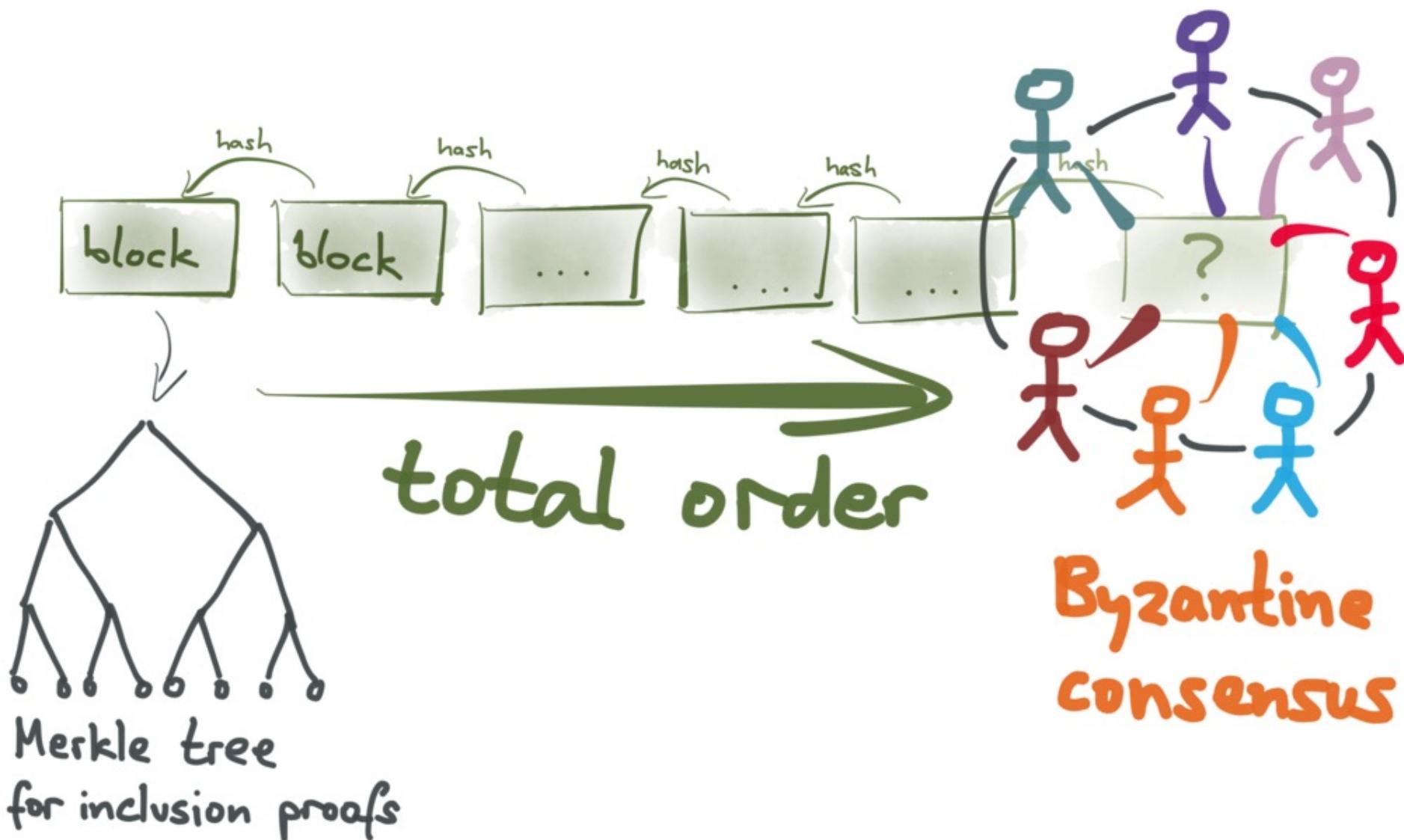




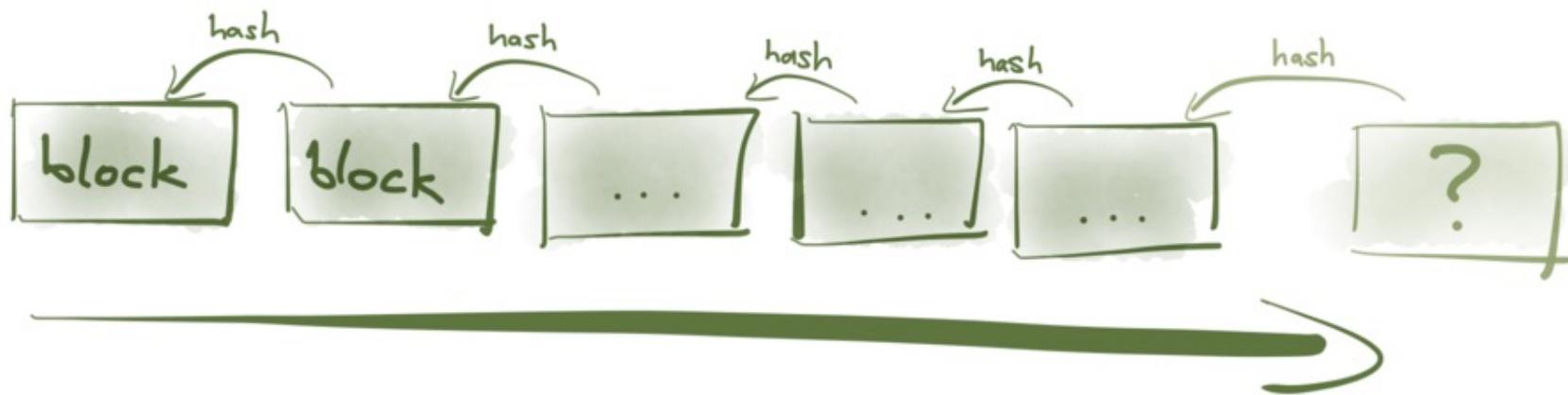
# BLOCKCHAIN TO THE RESCUE?



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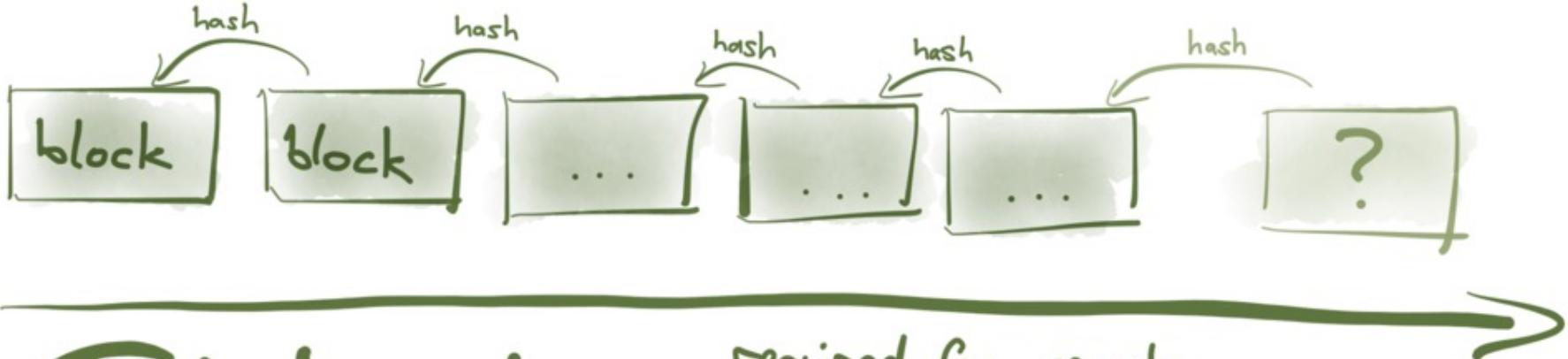


# BLOCKCHAIN TO THE RESCUE?



Total order required for cryptocurrencies  
(to prevent double-spending).

The wrong model for collaboration!

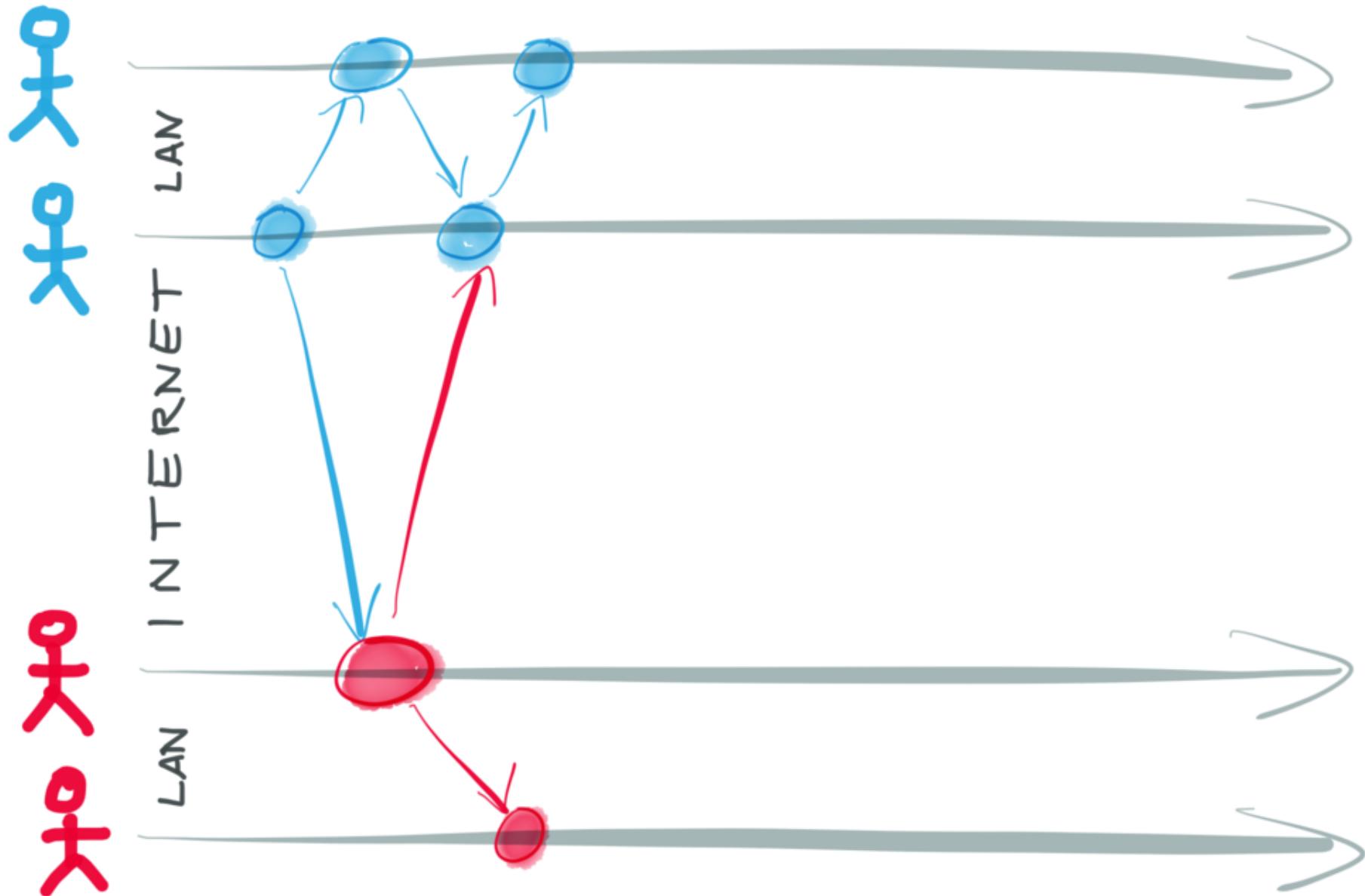


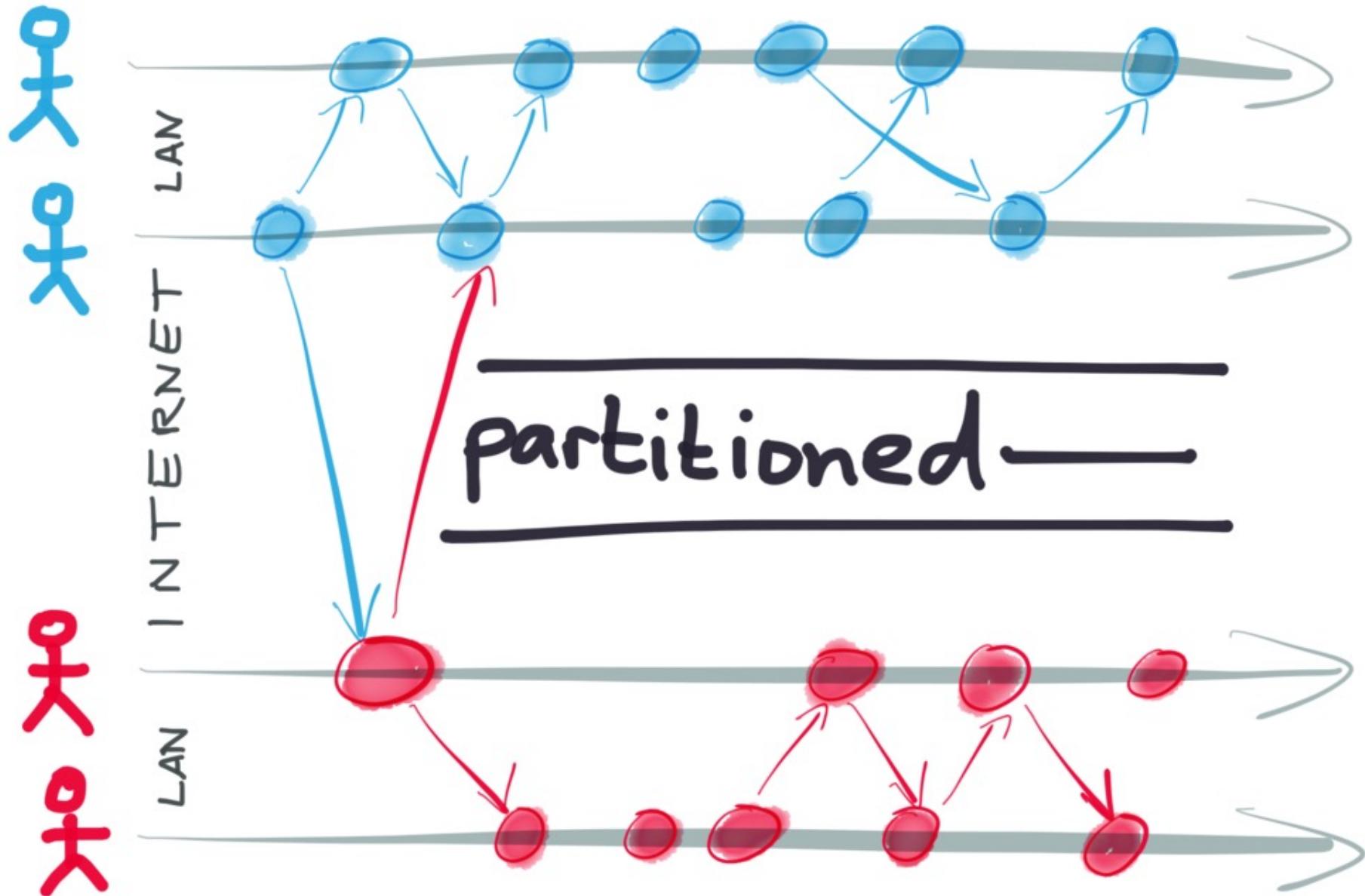
Total order

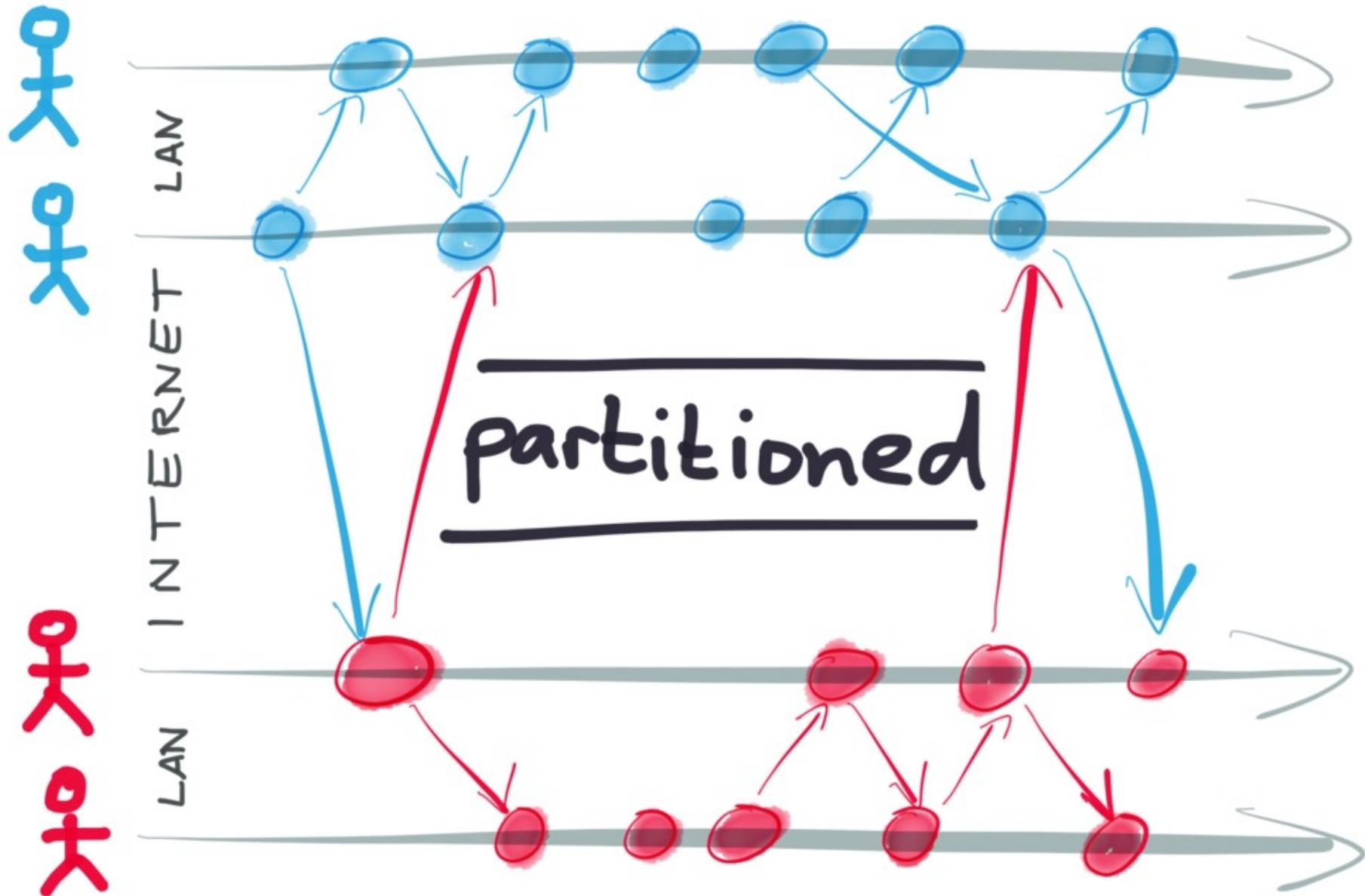
required for cryptocurrencies  
(to prevent double-spending)

Consensus = pick one of several proposed values

Collaboration = keep all edits and merge them







# Byzantine Eventual Consistency and the Fundamental Limits of Peer-to-Peer Databases

Martin Kleppmann  
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Cambridge, UK  
mk428@cst.cam.ac.uk

## ABSTRACT

Sybil attacks, in which a large number of adversary-controlled nodes join a network, are a concern for many peer-to-peer database systems, necessitating expensive countermeasures such as proof-of-work. However, there is a category of database applications that are, by design, immune to Sybil attacks because they can tolerate arbitrary numbers of Byzantine-faulty nodes. In this paper, we characterize this category of applications using a consistency model we call *Byzantine Eventual Consistency* (BEC). We introduce an algorithm that guarantees BEC based on Byzantine causal broadcast, prove its correctness, and demonstrate near-optimal performance in a prototype implementation.

## 1 INTRODUCTION

Peer-to-peer systems are of interest to many communities for a number of reasons: their lack of central control by a single party can make them more resilient, and less susceptible to censorship

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The reason why permissioned blockchains must control membership is that they rely on Byzantine agreement, which assumes that at most  $f$  nodes are Byzantine-faulty. To tolerate  $f$  faults, Byzantine agreement algorithms typically require at least  $3f + 1$  nodes [17]. If more than  $f$  nodes are faulty, these algorithms can guarantee neither safety (agreement) nor liveness (progress). Thus, a Sybil attack that causes the bound of  $f$  faulty nodes to be exceeded can result in the system's guarantees being violated; for example, in a cryptocurrency, they could allow the same coin to be spent multiple times (a *double-spending* attack).

This state of affairs raises the question: if Byzantine agreement cannot be achieved in the face of arbitrary numbers of Byzantine-faulty nodes, what properties *can* be guaranteed in this case?

A system that tolerates arbitrary numbers of Byzantine-faulty nodes is immune to Sybil attacks: even if the malicious peers outnumber the honest ones, it is still able to function correctly. This makes such systems of large practical importance: being immune to Sybil attacks means neither proof-of-work nor the central control of permissioned blockchains is required.

# Byzantine Eventual Consistency (BEC)

Eventual update:

One correct replica applies update  $u$

$\Rightarrow$  all correct replicas eventually apply  $u$

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The state of a correct replica always satisfies all of the app's declared invariants

(and a few other, more technical properties)

# VERSION VECTORS ARE NOT SAFE

correct



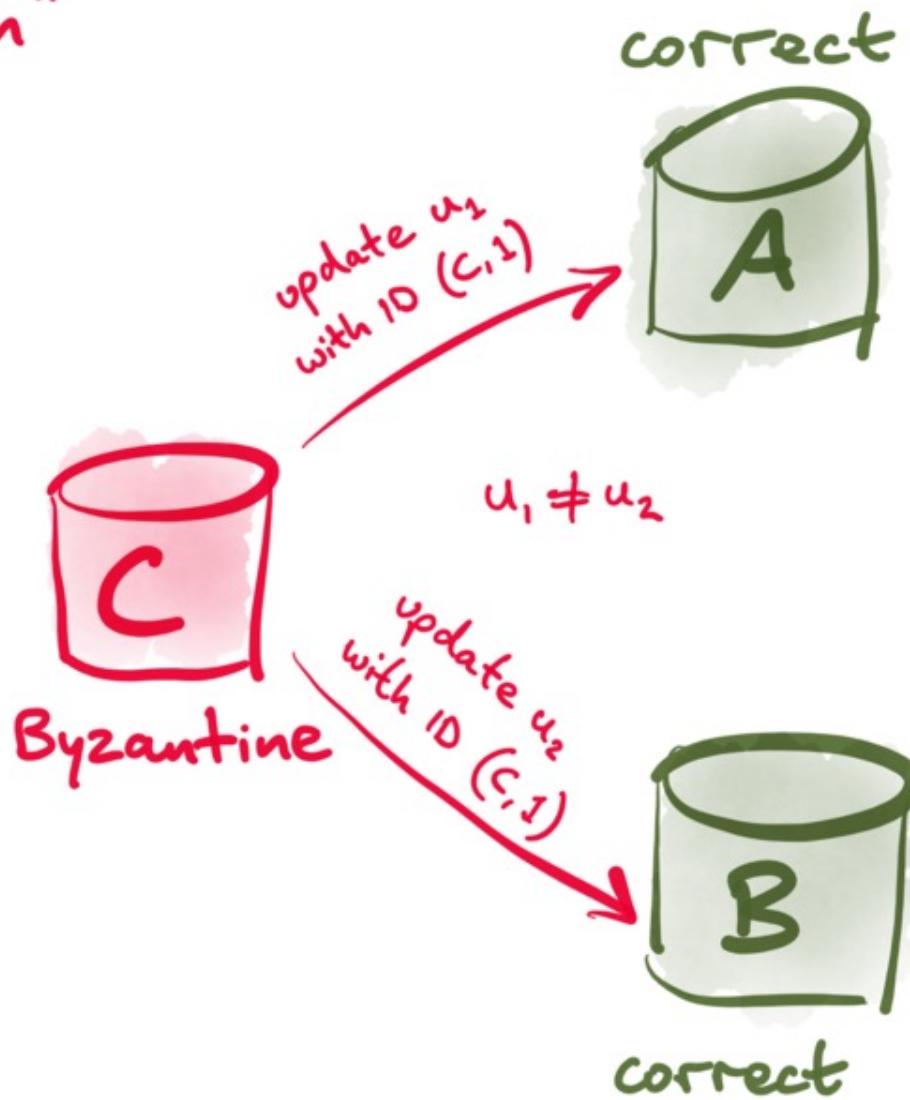
Byzantine



correct

# VERSION VECTORS ARE NOT SAFE

"equivocation"



# VERSION VECTORS ARE NOT SAFE

correct



$$\{(c, 1) \mapsto u_1\}$$



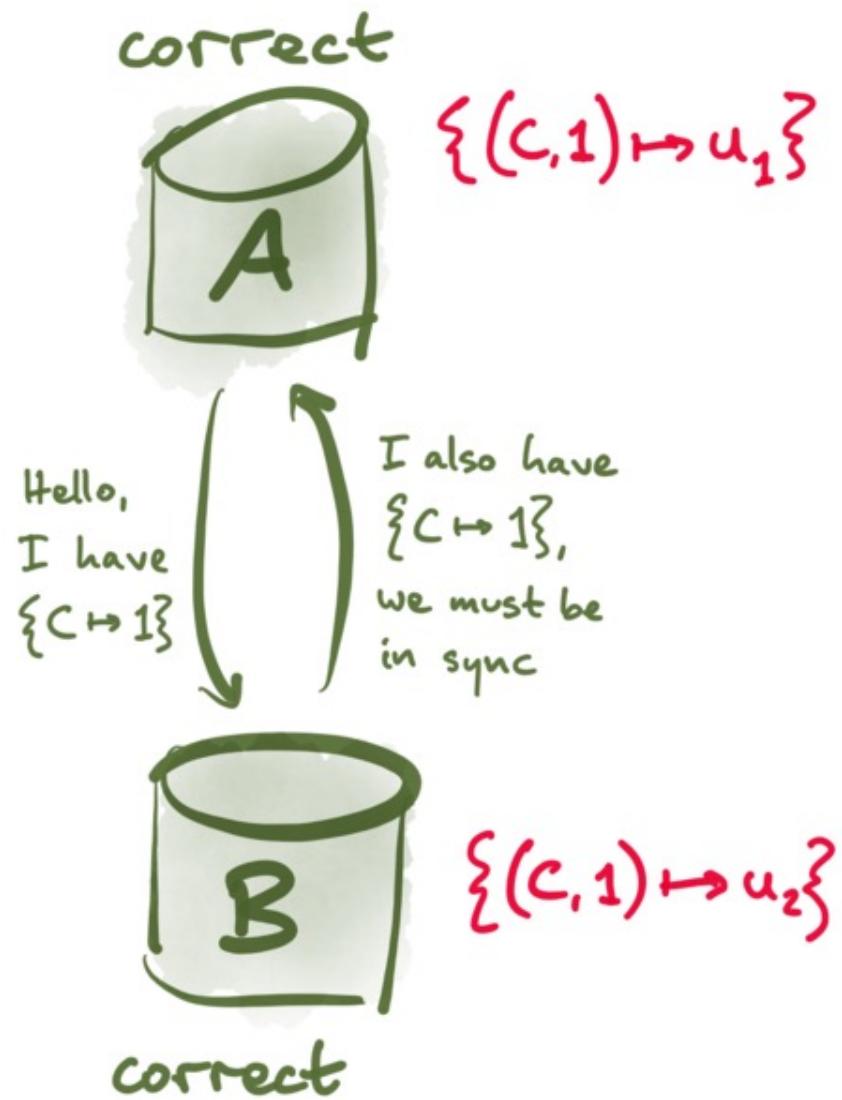
Byzantine



correct

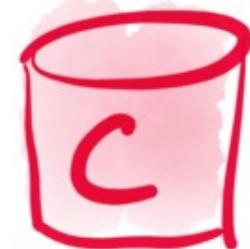
$$\{(c, 1) \mapsto u_2\}$$

# VERSION VECTORS ARE NOT SAFE



# VERSION VECTORS ARE NOT SAFE

A never delivers  $u_2$   
B never delivers  $u_1$   
 $\Rightarrow$  failure of eventual delivery



Byzantine

correct



$\{(C, 1) \mapsto u_1\}$

Hello,  
I have  
 $\{C \mapsto 1\}$

I also have  
 $\{C \mapsto 1\}$ ,  
we must be  
in sync



correct

$\{(C, 1) \mapsto u_2\}$

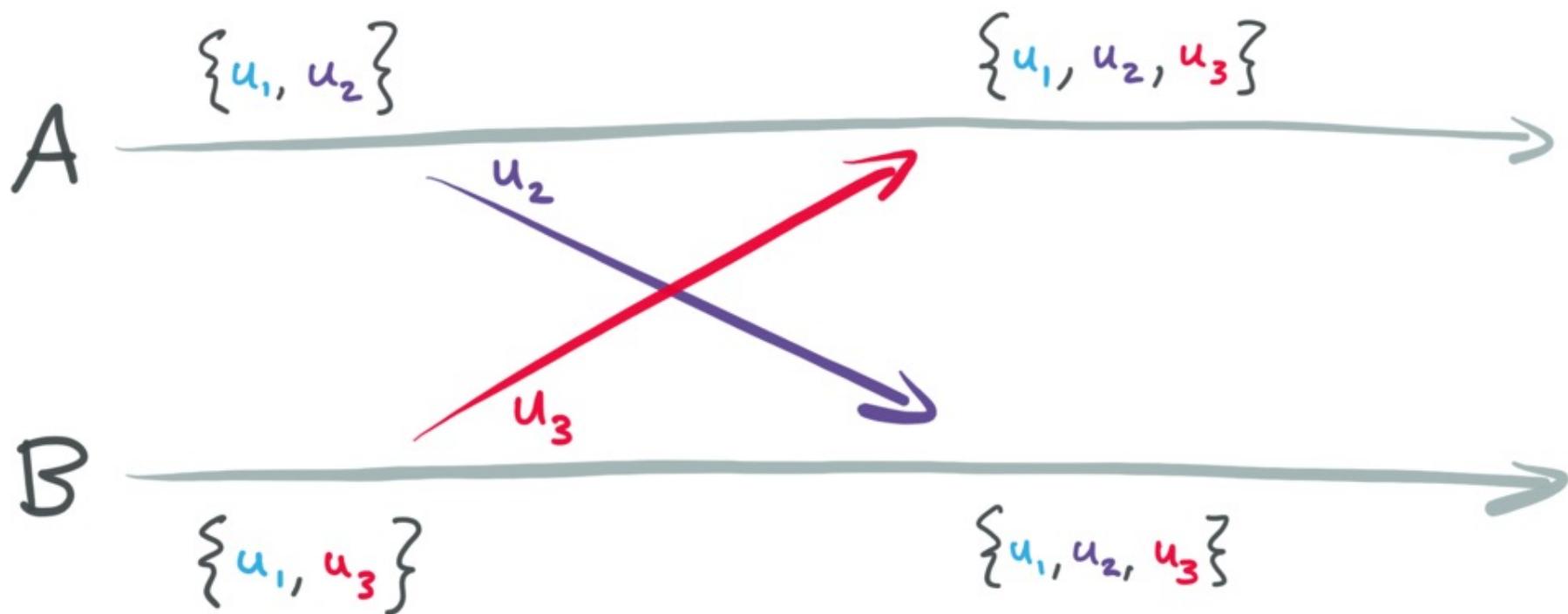
# ENSURING EVENTUAL DELIVERY

Nodes connect pairwise, send each other updates  
that the other doesn't have



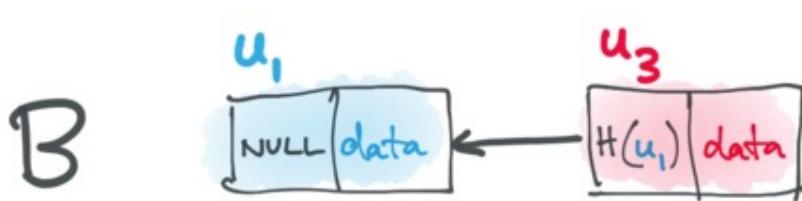
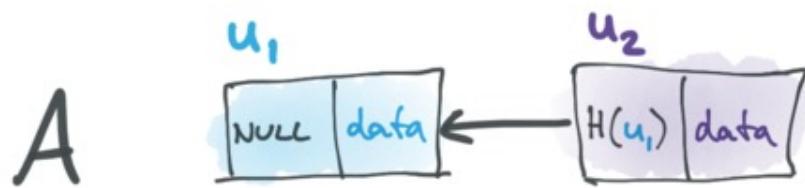
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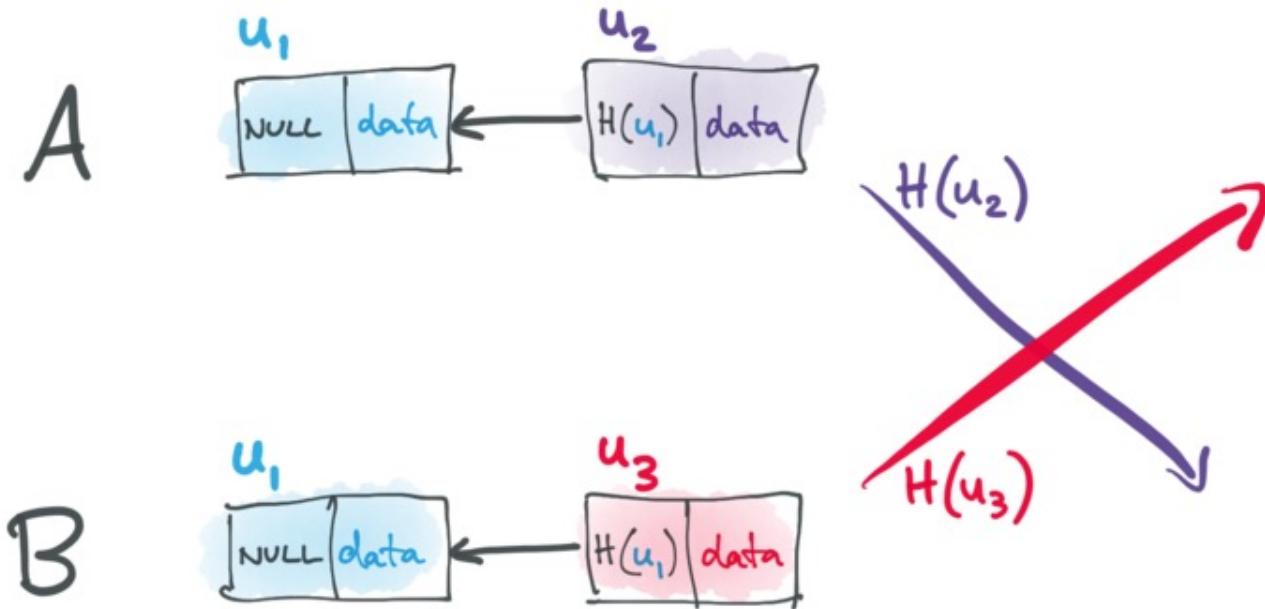
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How do nodes figure out what to send to each other?  
Hash graph (like Git!):



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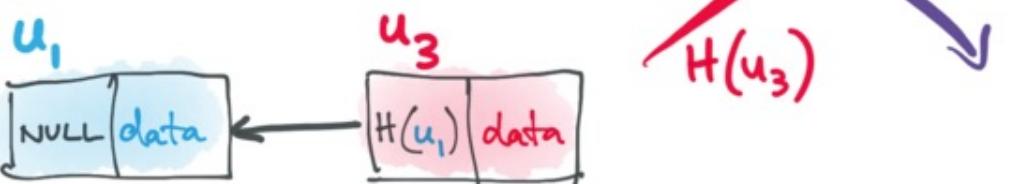
How do nodes figure out what to send to each other?

Hash graph (like Git!):

A



B

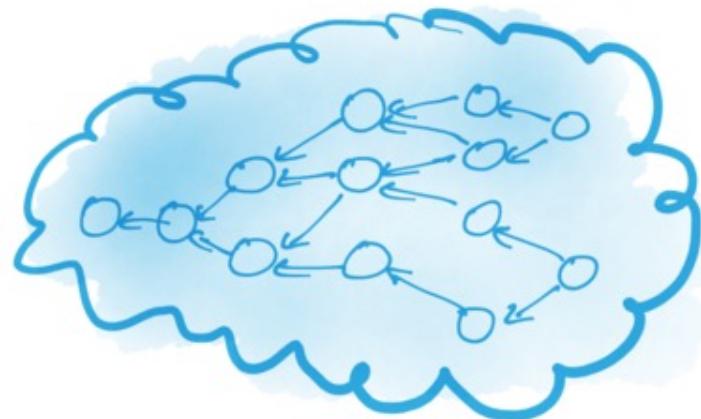


hash unknown?  
work backwards  
in hash DAG  
until known hash  
is found

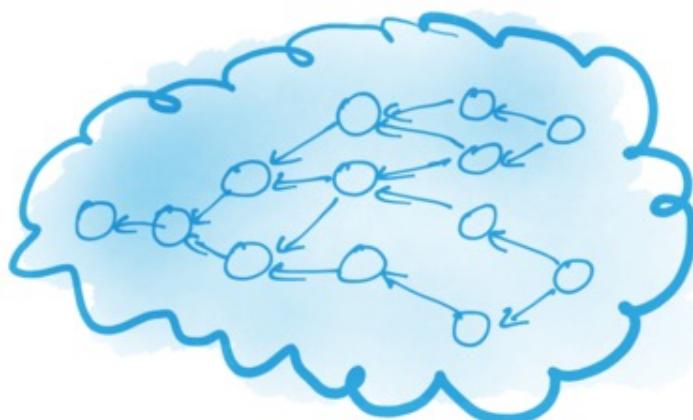
Assuming a collision-resistant hash function, a Byzantine node cannot cause two correct nodes to believe they are in sync when in fact they have diverged.

# BEC replication

A



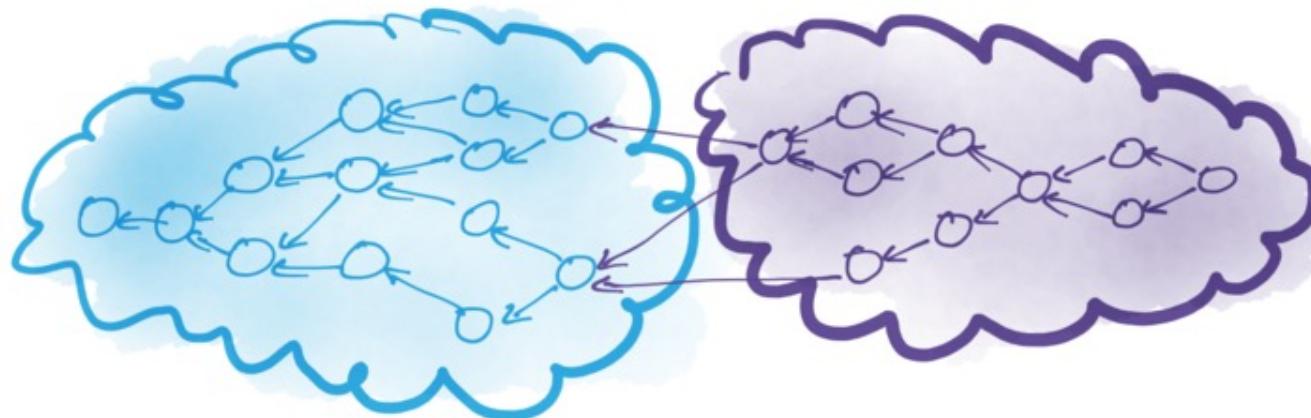
B



remember result of last sync between A and B

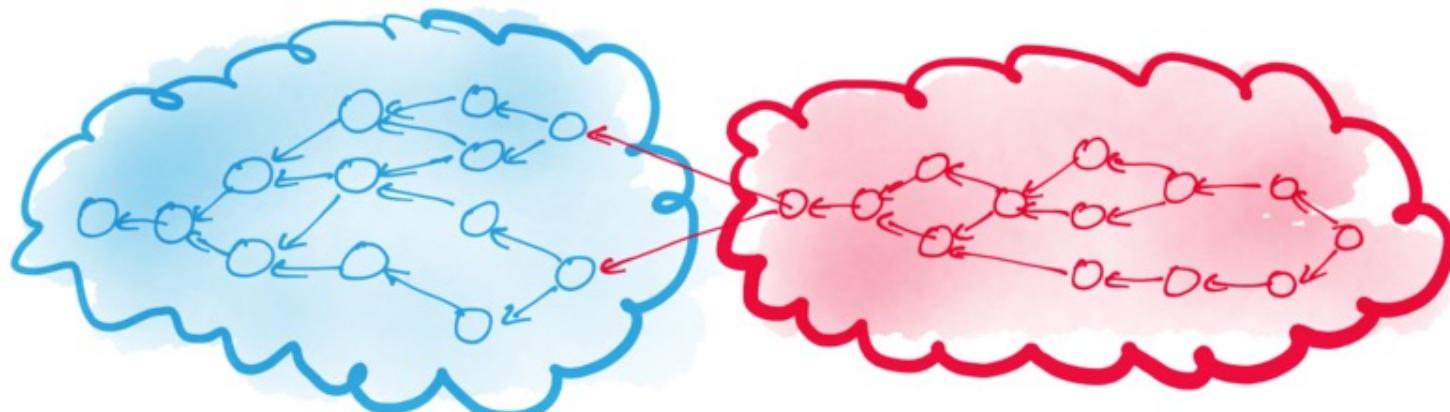
## BEC replication

A



added by A since last sync

B

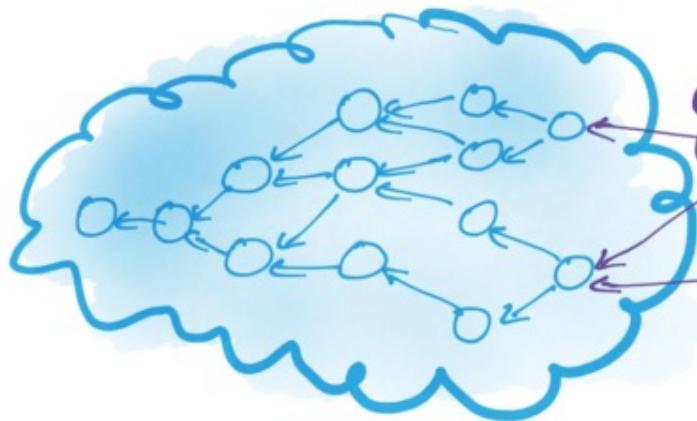


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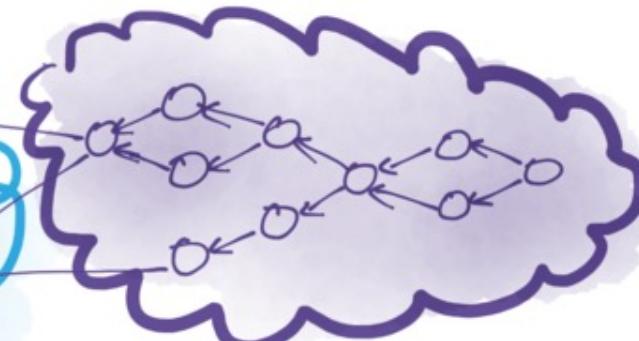
added by B since last sync

# BEC replication

A

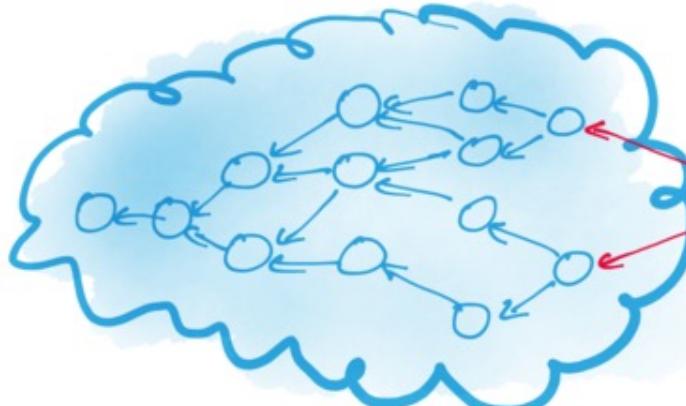


added by A since last sync

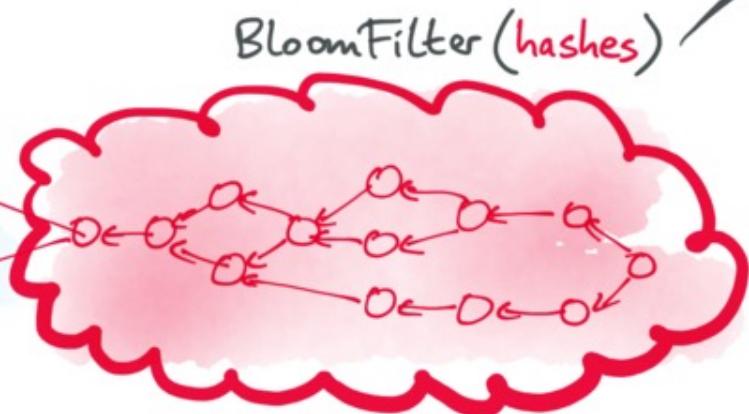


BloomFilter (hashes)

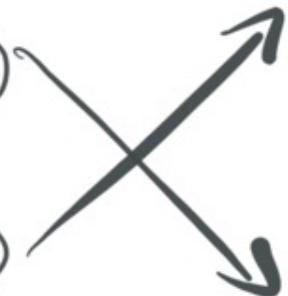
B



remember result of last sync between A and B



added by B since last sync



This sync protocol is implemented in Automerge  
[github.com/automerge/automerge](https://github.com/automerge/automerge)

Thanks to Peter van Hardenberg & other contributors!

Blog post

[martin.kleppmann.com/2020/12/02/  
bloom-filter-hash-graph-sync.html](https://martin.kleppmann.com/2020/12/02/bloom-filter-hash-graph-sync.html)

Details in the paper! [arxiv.org/abs/2012.00472](https://arxiv.org/abs/2012.00472)

# Byzantine Eventual Consistency (BEC)

Eventual update:

One correct replica applies update  $u$

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Convergence:  $\leftarrow$  use CRDTs

Two replicas have applied same set of updates

$\Rightarrow$  they are in the same state

Invariant preservation:

The state of a correct replica always satisfies all of the app's declared invariants

(and a few other, more technical properties)

Who are the current members of a group  
chat / collaborators on a document?

Simple answer: all users who have been added and not removed again  
Real answer: not as straightforward as you may think...

Work-in-progress with Annette Bieniusa and Herb Caudill

## Recovering from key compromise in decentralised access control systems

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Annette Bieniusa

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Kaiserslautern, Germany  
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**Abstract**—In systems with multiple administrators, such as group chat applications, it can happen that two users concurrently revoke each other’s permissions. For example, this could occur because an administrator’s device was compromised, and an adversary is actively using stolen credentials from this device while another administrator is trying to revoke the compromised device’s access. In decentralised systems, the order of these mutual revocations may be unclear, leading to disagreement about who the current group members are. We present an algorithm for managing groups where members can add or remove other members. In the event of a compromise, our algorithm allows the legitimate users to reliably revoke all compromised devices and lock out the adversary, regardless of how the adversary uses secret keys from the compromised devices. Our algorithm requires no trusted authority and no central control, and can therefore be used in decentralised settings such as mesh or mix networks.

**Index Terms**—access control, authorisation, group messaging, group membership, decentralisation, key compromise, CRDT

may sometimes fall into the hands of a malicious adversary. When this happens, the remaining users must be able to revoke the compromised credentials’ permissions, so as to limit the damage that the adversary can do.

The problem is: once the secret keys of an authorised user are in the hands of an adversary, the adversary may perform arbitrary actions pretending to be that user. For example, if Bob’s keys were compromised, and Alice (another authorised user) tries to revoke the permissions associated with Bob’s key, the adversary may try to first revoke Alice’s permissions and thus prevent her from removing the adversary’s access. Alternatively, the adversary may use Bob’s key to add several new devices that are also controlled by the adversary; thus, even if Bob’s key is revoked, the adversary may be able to continue accessing the system through one of these other devices, until they are also removed.

In some systems, it is possible to use a centralised arbiter, such as a trusted server, to resolve such conflicting permission changes. However, the problem becomes harder in decentralised systems that have no such central point of control: for example, mesh networks have been used by protesters to communicate without using the Internet [2].

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decentralised access control lists

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- Who may write some data?

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- Better: end-to-end encryption + decentralised access control lists

- Who may write some data?

- Centralised: server rejects unauthorised changes
- Decentralised: every peer maintains ACL, ignores changes from peers who don't have permission

Want a "decentralised access control list" protocol:

- Group creator is an admin
- Any admin can add/remove other admins

[Distinction between admins and non-admin group members elided for now]

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## Requirements

- No server, no trusted authority
- No infrastructure besides P2P networking (no blockchain)
- Must tolerate users being offline
- Non-admins cannot affect group state
- Everyone agrees who the admins are (eventually, after messages delivered)

## Approach



- Every user/device  $A$  has a keypair  $(pk_A, sk_A)$
- Operations: create group, add member, remove member
- Each operation is signed by its creator
- Signed operations are broadcast (e.g. by gossip protocol) to all group members
- $\text{currentMembers} = f(\text{operationsReceived})$  at each device

Users/devices: Alice, Bob, Carol, Dave, ...

Public keys:  $pk_A, pk_B, pk_C, pk_D, \dots$

Private keys:  $sk_A, sk_B, sk_C, sk_D, \dots$

$op_1 = (\text{create}, pk_A)$   
 $\text{Sign}(op_1, sk_A)$

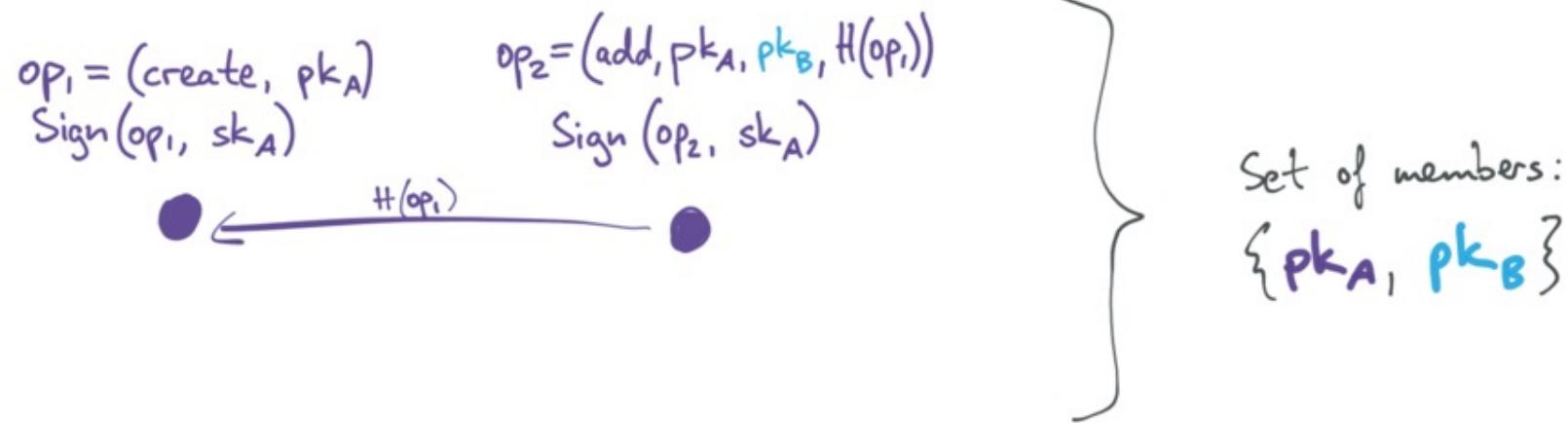


Set of members:  
 $\{pk_A\}$

Users/devices: Alice, Bob, Carol, Dave, ...

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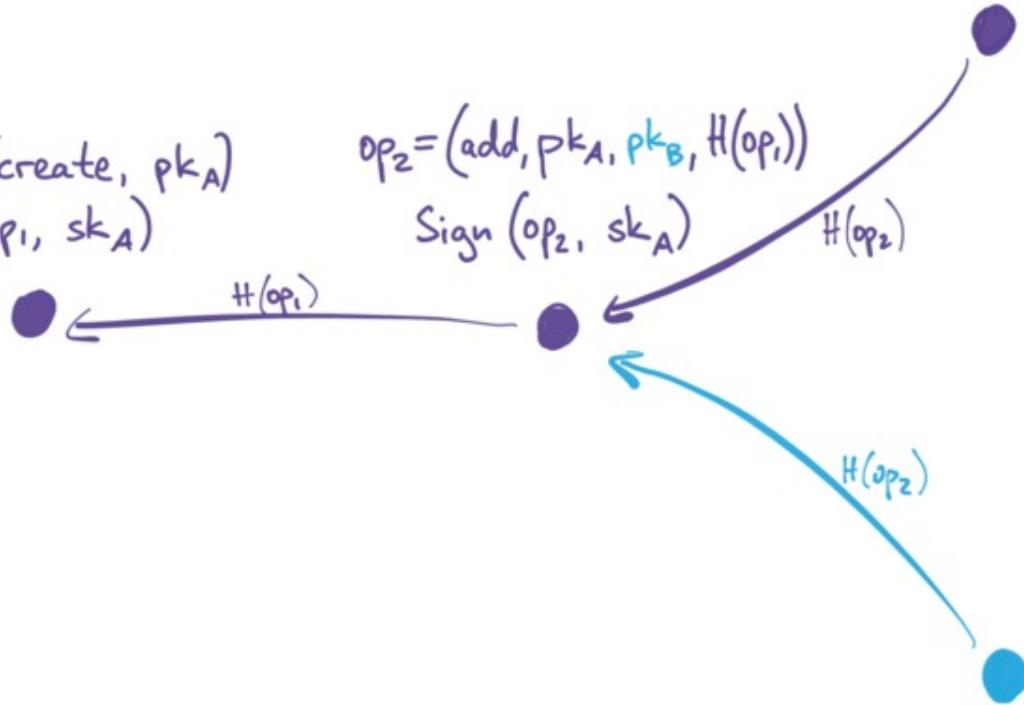
Public keys:  $pk_A, pk_B, pk_C, pk_D, \dots$

Private keys:  $sk_A, sk_B, sk_C, sk_D, \dots$

$$op_3 = (add, pk_A, \textcolor{red}{pk_C}, H(op_2)) \\ \text{Sign}(op_3, sk_A)$$

$$op_1 = (\text{create}, pk_A) \\ \text{Sign}(op_1, sk_A)$$

$$op_2 = (add, pk_A, pk_B, H(op_1)) \\ \text{Sign}(op_2, sk_A) \\ H(op_2)$$



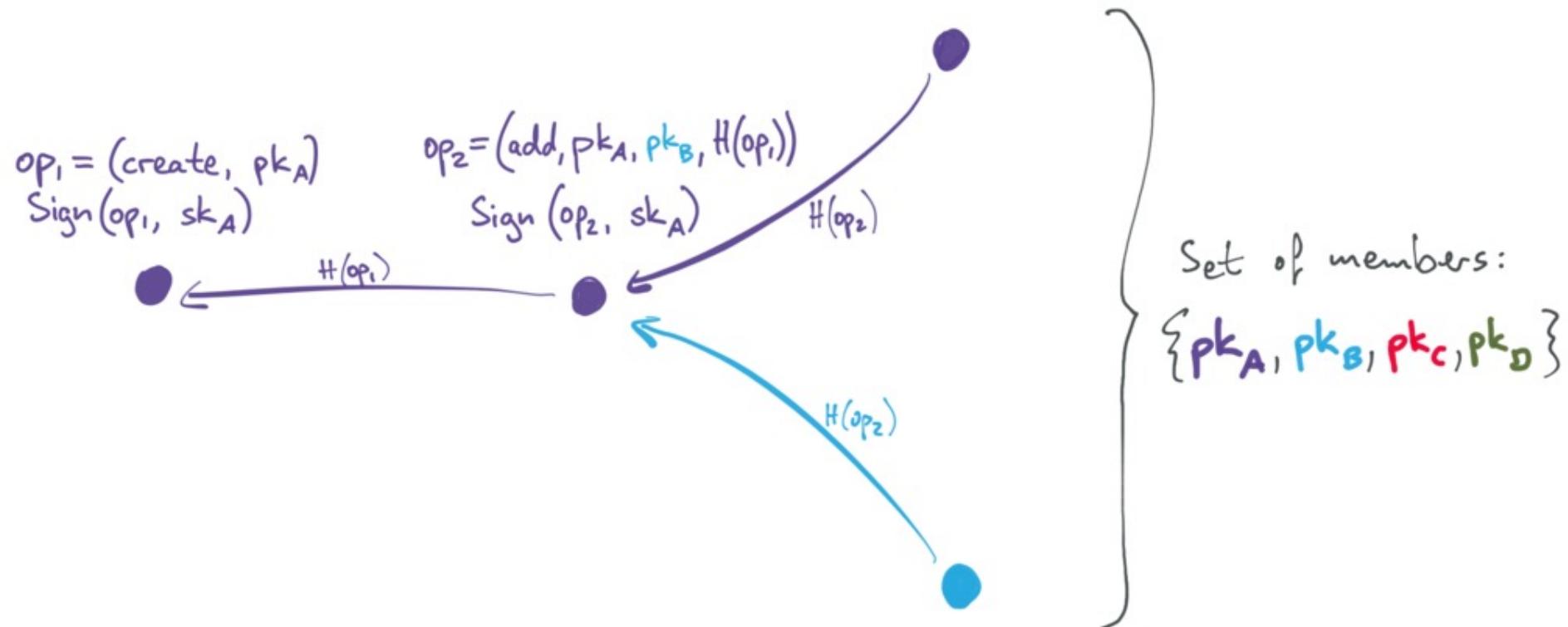
$$op_4 = (add, pk_B, pk_D, H(op_2)) \\ \text{Sign}(op_4, sk_B)$$

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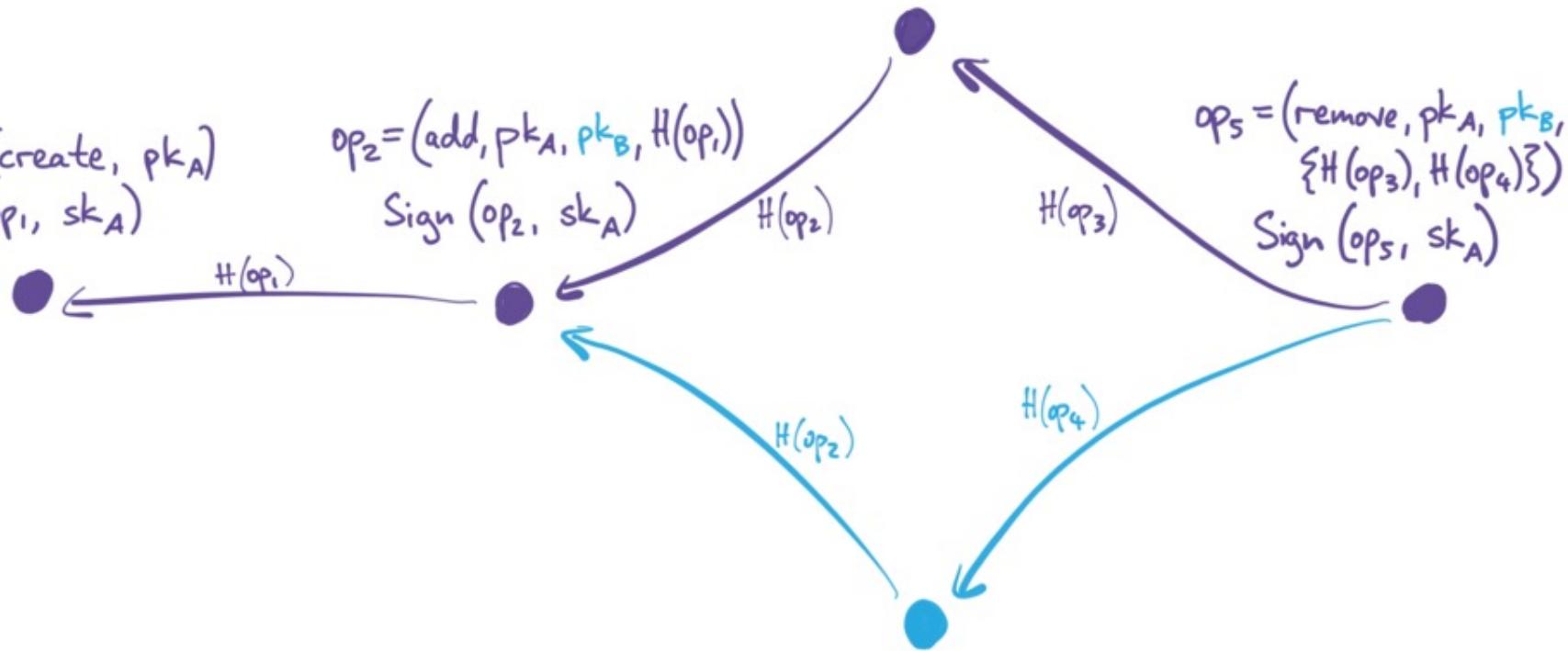
Private keys:  $sk_A, sk_B, sk_C, sk_D, \dots$

$$op_3 = (\text{add}, pk_A, \cancel{pk_C}, H(op_2)) \\ \text{Sign}(op_3, sk_A)$$

$$op_1 = (\text{create}, pk_A) \\ \text{Sign}(op_1, sk_A)$$

$$op_2 = (\text{add}, pk_A, pk_B, H(op_1)) \\ \text{Sign}(op_2, sk_A)$$

$$op_5 = (\text{remove}, pk_A, pk_B, \{H(op_3), H(op_4)\}) \\ \text{Sign}(op_5, sk_A)$$



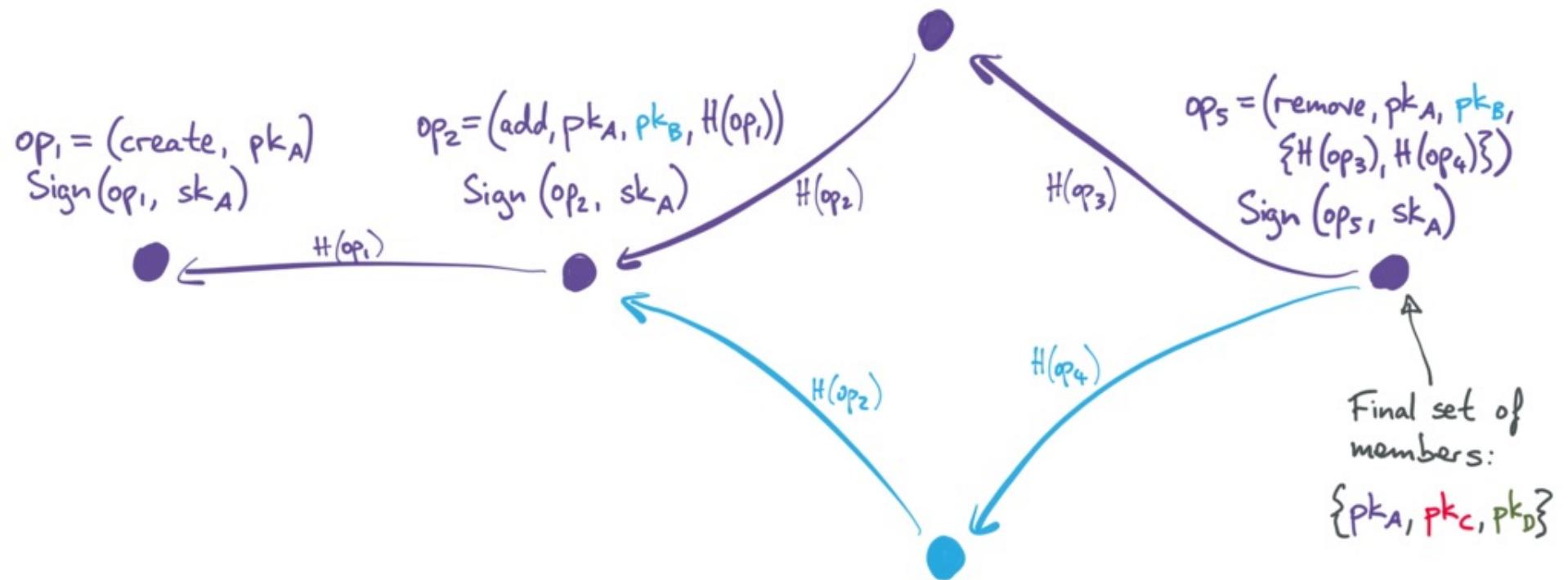
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$$op_3 = (\text{add}, pk_A, \cancel{pk_C}, H(op_2)) \\ \text{Sign}(op_3, sk_A)$$



$$op_4 = (\text{add}, pk_B, pk_D, H(op_2)) \\ \text{Sign}(op_4, sk_B)$$

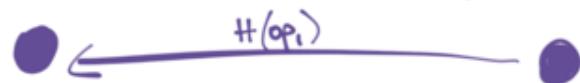
NOTE:  $pk_D$  is a member because it was added by B at a time when B was still a member.

Problem: what if you want to remove the permissions from someone who doesn't want to be removed? (Byzantine behaviour)

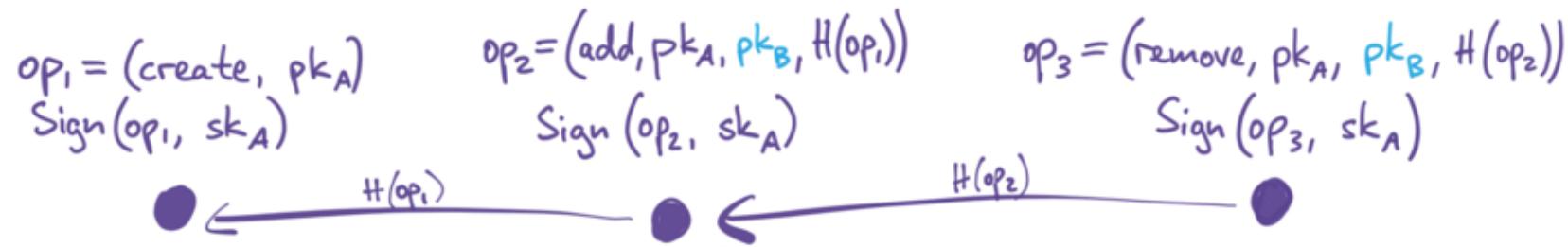
e.g. adversary stole + unlocked a team member's phone

A removed user concurrently  
adds a new user...

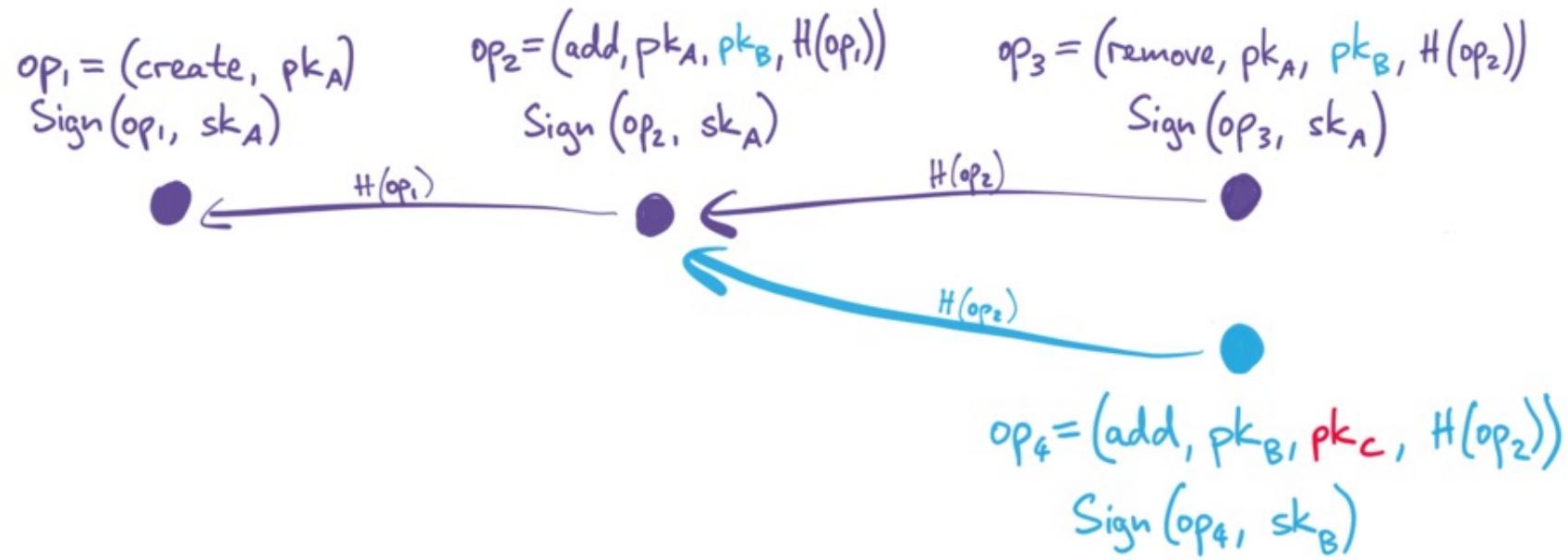
$$\begin{array}{ll} op_1 = (create, pk_A) & op_2 = (add, pk_A, pk_B, H(op_1)) \\ \text{Sign}(op_1, sk_A) & \text{Sign}(op_2, sk_A) \end{array}$$



A removed user concurrently  
adds a new user...

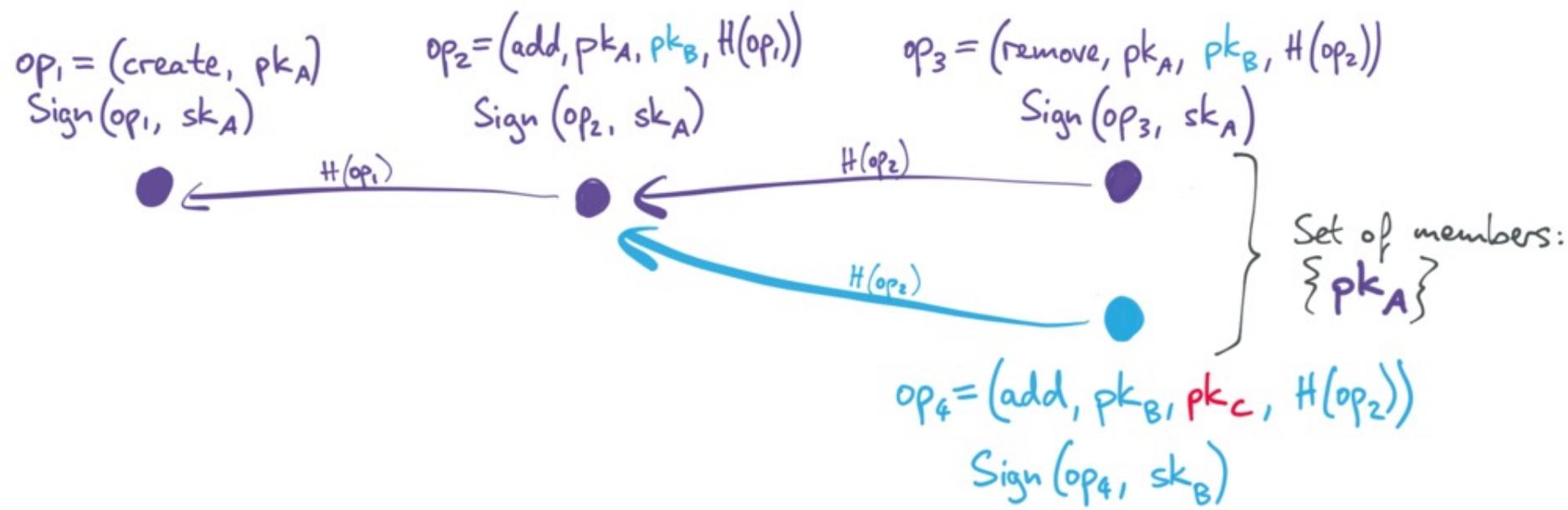


A removed user concurrently adds a new user...



B's operation to add C can be back-dated to appear concurrent with A's removal of B.

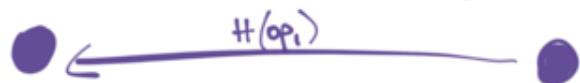
A removed user concurrently adds a new user...



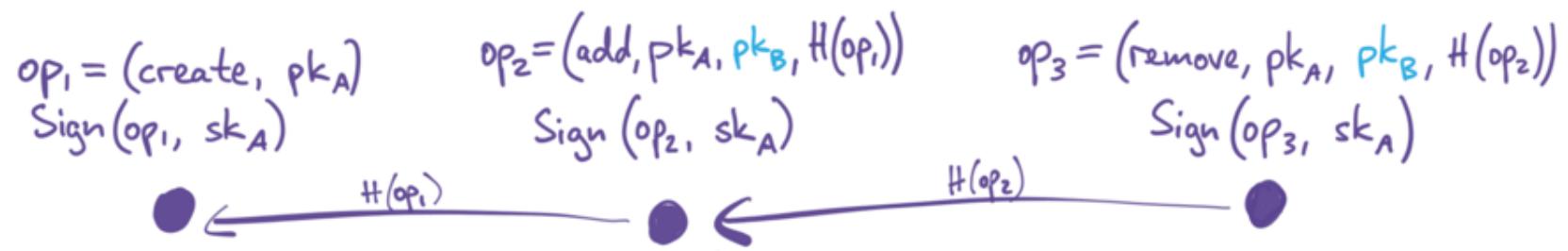
B's operation to add C can be back-dated to appear concurrent with A's removal of B.  
⇒ ignore all ops by B concurrent with removal of B

Two users concurrently  
remove each other...

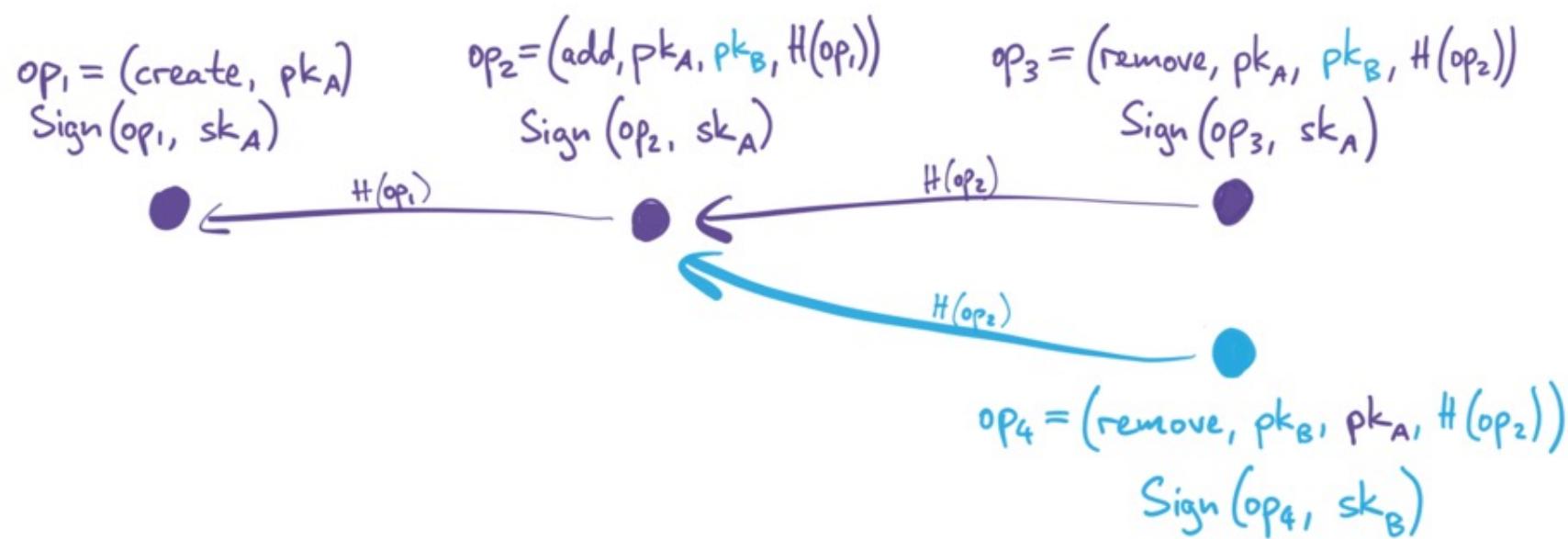
$$\begin{array}{ll} op_1 = (create, pk_A) & op_2 = (add, pk_A, pk_B, H(op_1)) \\ \text{Sign}(op_1, sk_A) & \text{Sign}(op_2, sk_A) \end{array}$$



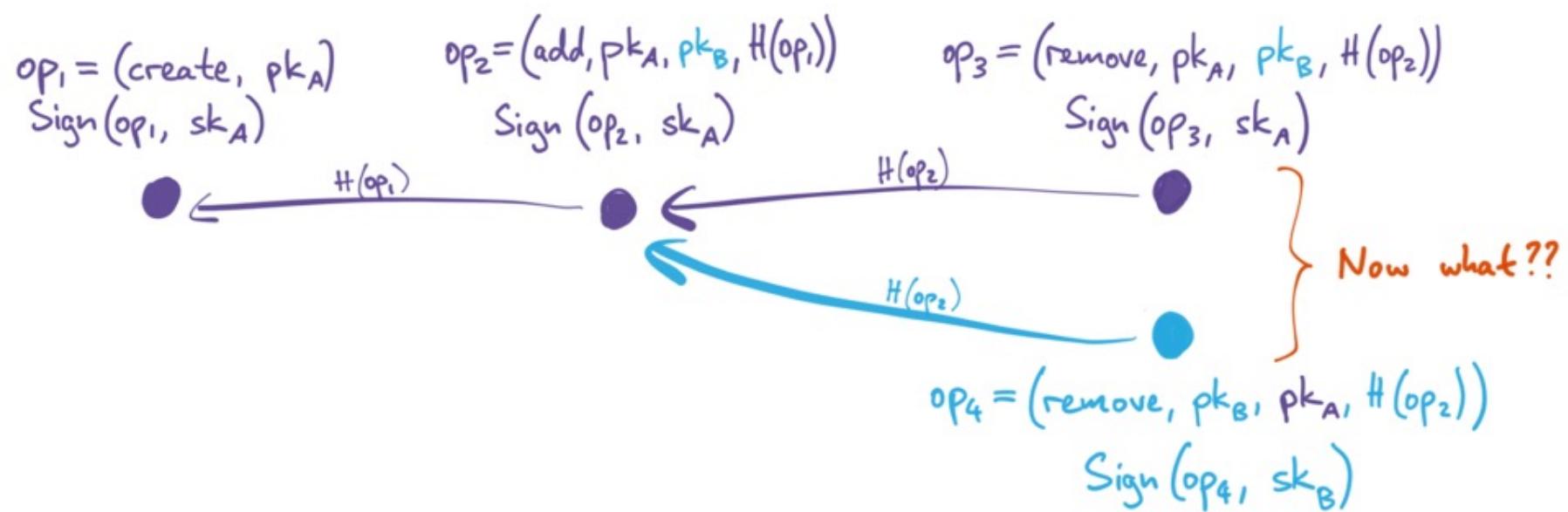
Two users concurrently  
remove each other...



Two users concurrently  
remove each other...

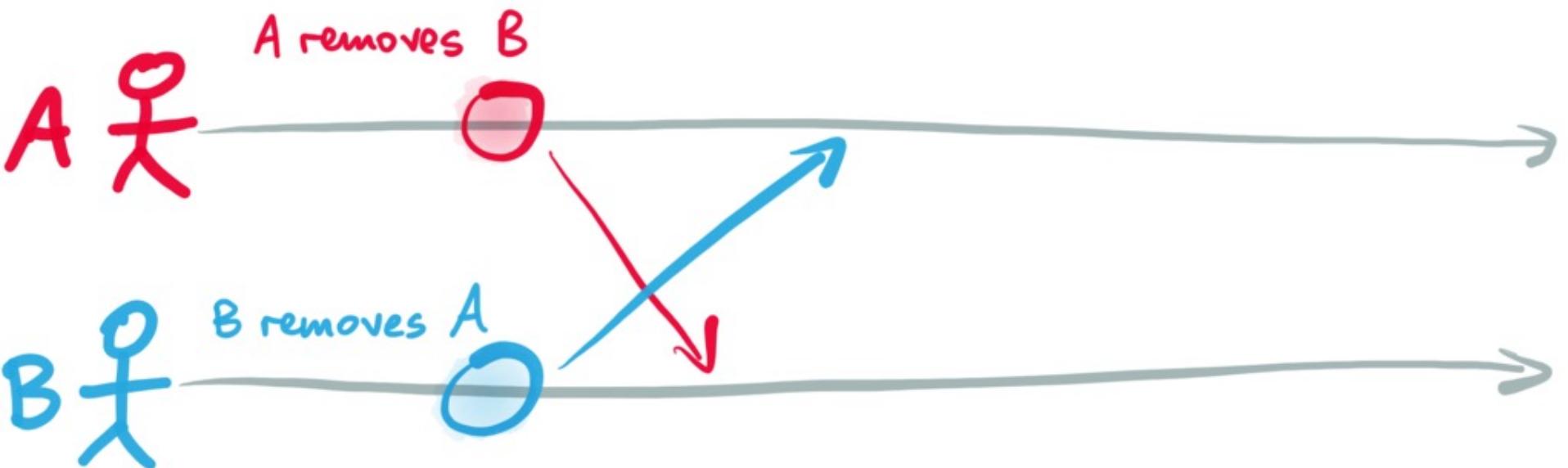


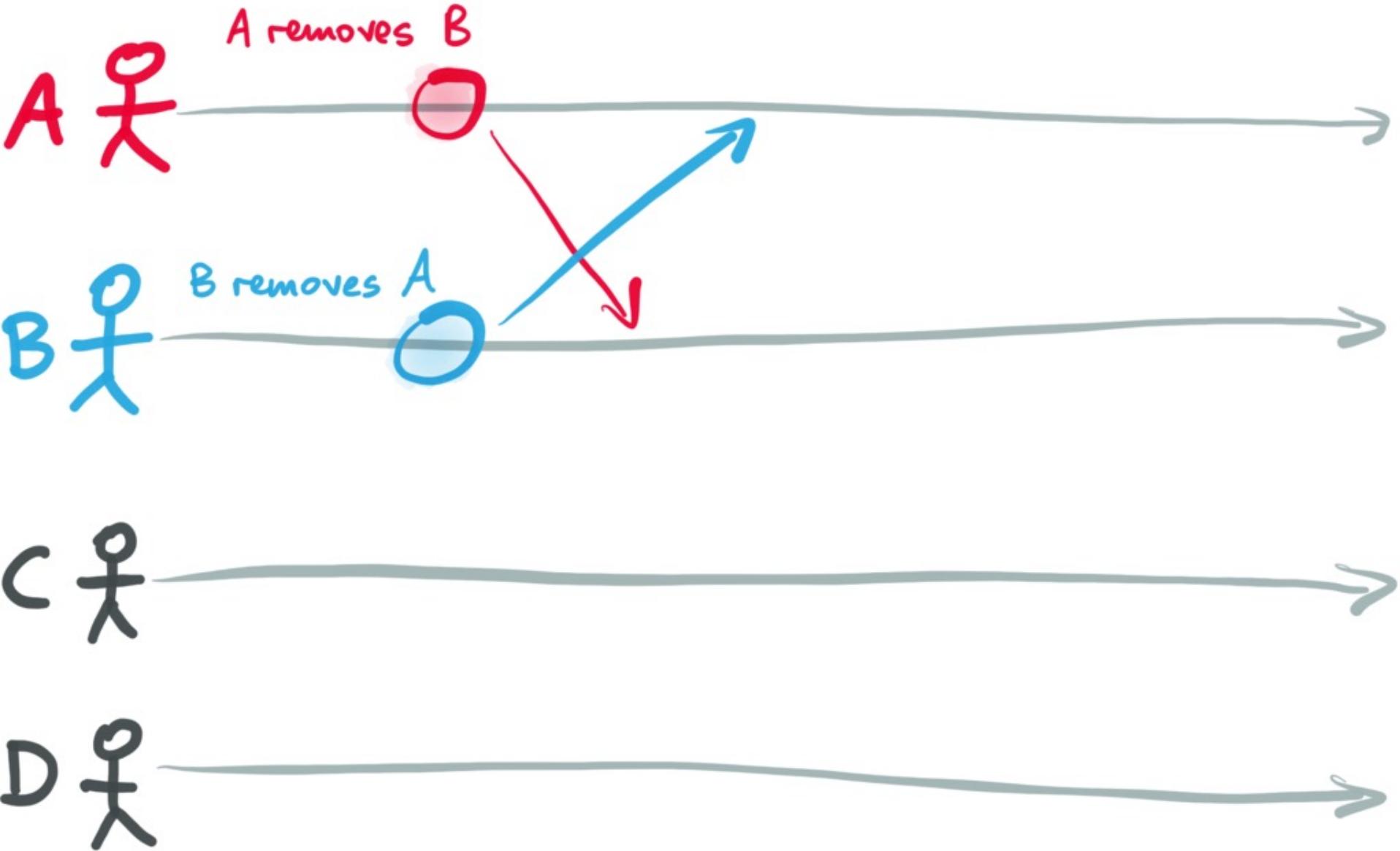
Two users concurrently  
remove each other...

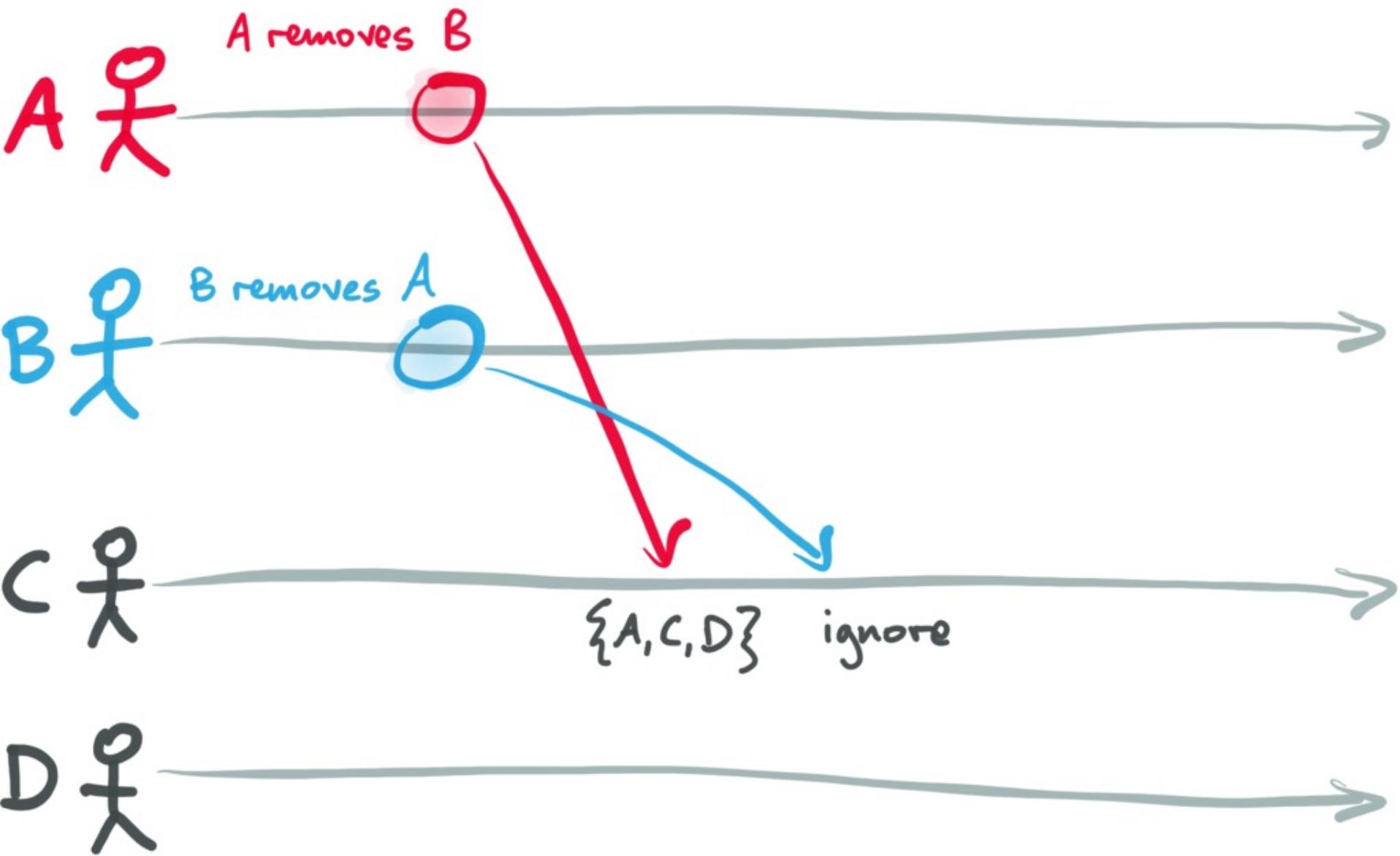


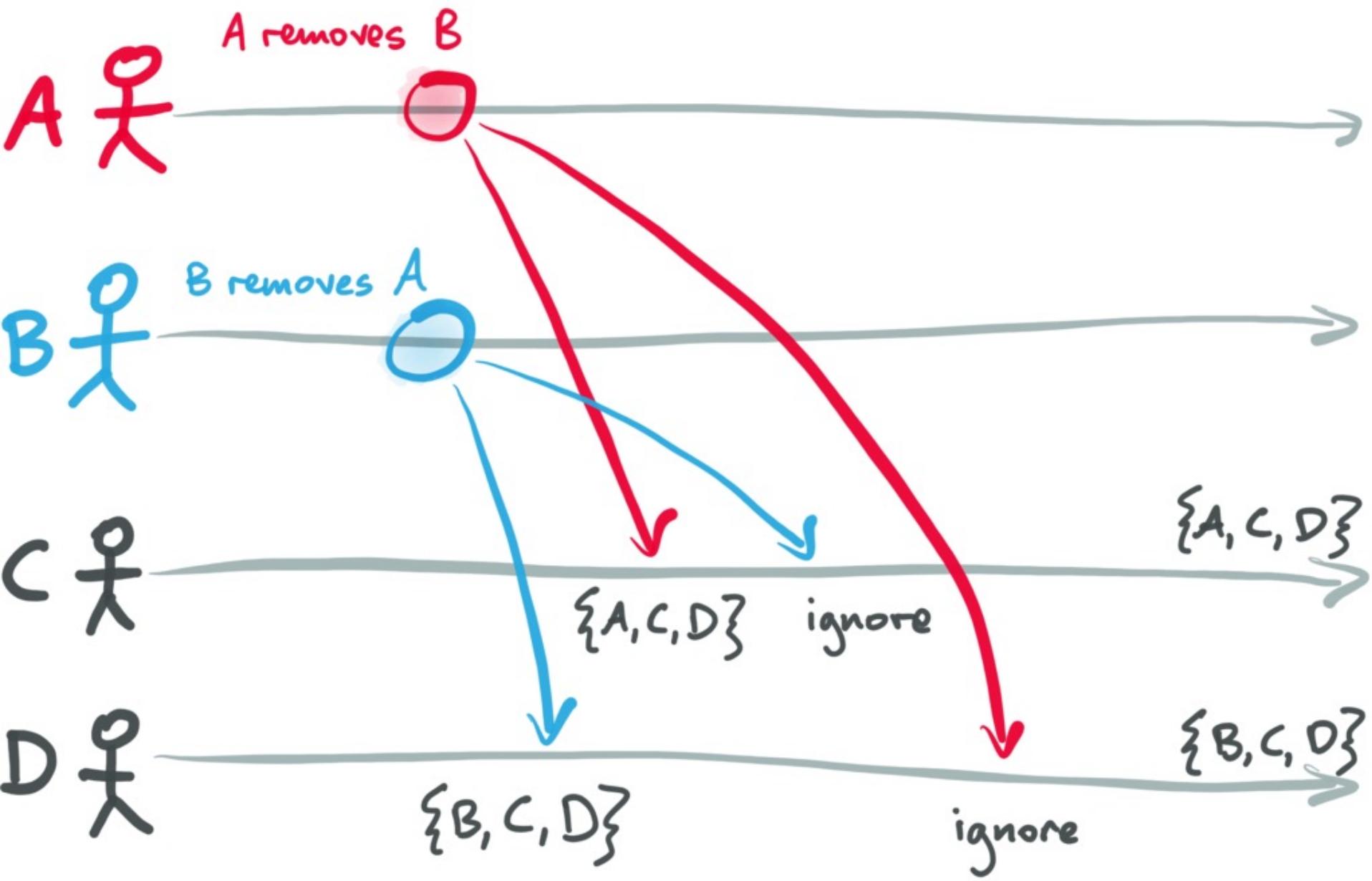
A 天

B 天









How to handle mutual revocation?

Operation timestamps?

How to handle mutual revocation?

~~Operation timestamps?~~ Adversarially chosen timestamps

Remove both?

How to handle mutual revocation?

~~Operation timestamps?~~ Adversarially chosen timestamps

~~Remove both?~~ DoS: might remove all admins

Remove neither?

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Trusted server as arbiter?

How to handle mutual revocation?

~~Operation timestamps?~~ Adversarially chosen timestamps

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Blockchain smart contract?

How to handle mutual revocation?

~~Operation timestamps?~~ Adversarially chosen timestamps

~~Remove both?~~ DoS: might remove all admins

~~Remove neither?~~ User can cancel their removal

~~Trusted server as arbiter?~~ Not decentralised

~~Blockchain smart contract?~~ How do you ensure control over smart contract is consistent with the ACL?

What do you do while waiting for blockchain decision?

# How to handle mutual revocation?

A

## Seniority ranking of users

e.g. group creator has rank 1, user added by rank- $i$  user has rank  $i+1$ ,  
break ties by lexicographic order on hashes of operations that added the users

Problem: how do you remove the most senior user?

# How to handle mutual revocation?

A

## Seniority ranking of users

e.g. group creator has rank 1, user added by rank- $i$  user has rank  $i+1$ ,  
break ties by lexicographic order on hashes of operations that added the users

Problem: how do you remove the most senior user?

B

## Users vote on who is right

Problems:

- who gets a vote? Sybil attack prevention needed
- how does a user know the correct answer?
- risk of social engineering attacks
- what happens while waiting for vote to complete?

# How to handle mutual revocation?

A

Seniority ranking of users

Problem: how do you remove the most senior user?

Solution:

Most senior public key is not for a single user/device, but rather a public key for a threshold signature scheme where the group members hold secret shares

⇒ k out of n users can override seniority ranking

⇒ need scheme for redistributing secret shares after group membership changes

# Byzantine Eventual Consistency (BEC)

Eventual update:

One correct replica applies update  $u$

$\Rightarrow$  all correct replicas eventually apply  $u$

Convergence:  $\leftarrow$  use CRDTs

Two replicas have applied same set of updates

$\Rightarrow$  they are in the same state

Invariant preservation:

The state of a correct replica always satisfies all of the app's declared invariants

(and a few other, more technical properties)

# References

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- More at <https://martin.kleppmann.com>